# Physics 1A, Section 2

November 1, 2010

### Office Hours

- Office hours will now be:
  - ✤ Tuesday, 3:30 5:00 PM (half an hour later)
  - still in Cahill 312

## Today's Agenda

- Finish energy problem from Thursday
- forces and potential energy
- potential energy of a fictitious force?
- potential energy applied to orbits
  - Lagrange points for Sun/Earth/satellite

### Quiz Problem 50



A block of mass m starts at rest and slides down a frictionless circular ramp from a height h. At the bottom, it hits a massless spring with spring constant k and in addition begins to experience a frictional force. The coefficient of kinetic friction is given by  $\mu$ .

- (1 point) (a) What is the speed of the block at the bottom of the ramp just before it hits the spring?
- (2 points)(b) Find the total horizontal force on the mass after it hits the spring as a function of the coordinate x given in the diagram.

The mass first comes to rest instantaneously at  $x=x_s$ . It then rebounds back up the ramp, reaching a maximum height h' < h. In the following, express your answer in terms of  $x_s$ :

- (2 points) (c) What is the total work done on the mass by the spring and friction between x=0 and x=x<sub>s</sub>?
- (2 points) (d) What is the total energy  $W_f$  that has been dissipated by friction when the spring first returns to x=0?
- (2 points) (e) Find the vertical height h' up the ramp to which the block rebounds. You may express your answer in terms of W<sub>f</sub>.

(1 point) (f) Find  $x_5$  in terms of the quantities shown above.

## Quiz Problem 50

- Answer:
- a) v = sqrt(2gh)
- b)  $F = -kx \mu mg$ , to the right
- c) W =  $-kx_s^2/2 \mu mgx_s$
- d)  $W_f = 2\mu mgx_s$
- e) h' = h  $2\mu x_s$
- f)  $x_s = [-\mu mg + sqrt(\mu^2 m^2 g^2 + 2kmgh)]/k$



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#### Conservative and Non-Conservative Forces

- $\bullet$  A conservative force **F** can be associated with a potential energy U
  - F = -dU/dr or -dU/dx in Physics 1a
    - ♦  $\mathbf{F} = (-\partial U/\partial x, -\partial U/\partial y, -\partial U/\partial z)$  more generally
  - Force is a function of position only.
  - example: uniform gravity: U = mgz
  - \* example: Newtonian gravity: U = -GMm/r
  - \* example: ideal spring:  $U = kx^2/2$
- ✤ Non-conservative forces
  - friction: force depends on direction of motion
  - normal force: depends on other forces
    - but does no work because it has no component in direction of motion.



#### Potential Energy from a Fictitious (Inertial) Force

It can be useful to associate the centrifugal force in a rotating frame with a potential energy:

•  $F_{centrifugal} = m\omega^2 r$  (outward)

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 (outward)

$$\Rightarrow U_{\text{centrifugal}} = -m\omega^2 r^2/2$$

#### Consider circular orbits (again)

- ✤ Work in the rotating (non-inertial) frame.
- planet orbiting the Sun:
  - $U_{tota1} = U_{gravity} + U_{centrifuga1}$

\* Equilibrium where 
$$dU_{total}/dr = 0 \implies GM_{Sun} = \omega^2 r^3$$

#### Consider circular orbits (again)

- ✤ Work in the rotating (non-inertial) frame.
- \* planet orbiting the Sun ( $M_{planet} << M_{sun}$ ):
  - $U_{total} = U_{gravity} + U_{centrifugal}$
  - \* Equilibrium where  $dU_{total}/dr = 0 \implies GM_{Sun} = \omega^2 r^3$
- ✤ Satellite and Earth orbiting the Sun (M<sub>satellite</sub> << M<sub>Earth</sub> << M<sub>Sun</sub>)
  - $U_{total} = U_{gravity,Sun} + U_{gravity,Earth} + U_{centrifugal}$
  - Equilibria at 5 Lagrange points

# Sun-Earth Lagrange Points



image from wikipedia

#### Location of Lagrange points

- L1,L2:  $\Delta R \approx R(M_E/3M_S)^{1/3}$ 
  - ✤ about 0.01 A.U. from Earth toward or away from Sun
  - unstable equilibria
- L3: orbital radius  $\approx R[1 + (5M_E/12M_s)]$ 
  - very unstable equilibrium
- ✤ L4,L5: three bodies form an equilateral triangle
  - stable equilibria (via Coriolis force)

1 A.U. = astronomical unit = distance from Earth to Sun





### Thursday, November 4:

Quiz Problem 38 (collision)

Optional, but helpful, to try this in advance.