

# CCAT Optical Design Trade-off Study

$f_1/0.6$  vs.  $f_1/0.4$

CCAT



Germán Cortés-Medellín

National Astronomy and Ionosphere Center



Cornell University



# Outline

- ◆ Main Optics Image Quality Impact
- ◆ Sub Reflector Positioning Impact
- ◆ Re-Imaging Optics Impact
- ◆ Active Surface Segment Positioning Errors Impact
- ◆ SCUBA-II/SW/LW Cameras Location

# Ritchey-Chrétien Design Parameters

$f_1/0.6$  vs.  $f_1/0.4$



**Design: Ritchey-Chrétien/Nasmyth Focus**

## Derived Design Parameters

### M1

Diameter  
Eccentricity  
Vertex Radius of Curvature  
Focal Distance  
Edge Angle from Prime Focus

Symbol	$f_1/0.6$	$f_1/0.4$	Units
$D_1$	25	25	[m]
$\varepsilon_1$	1.000774	1.000278	
$R_{C1}$	30.000	20.000	[m]
$f_1$	15.000	10.000	[m]
$\theta_1$	45.24	64.01	[deg]

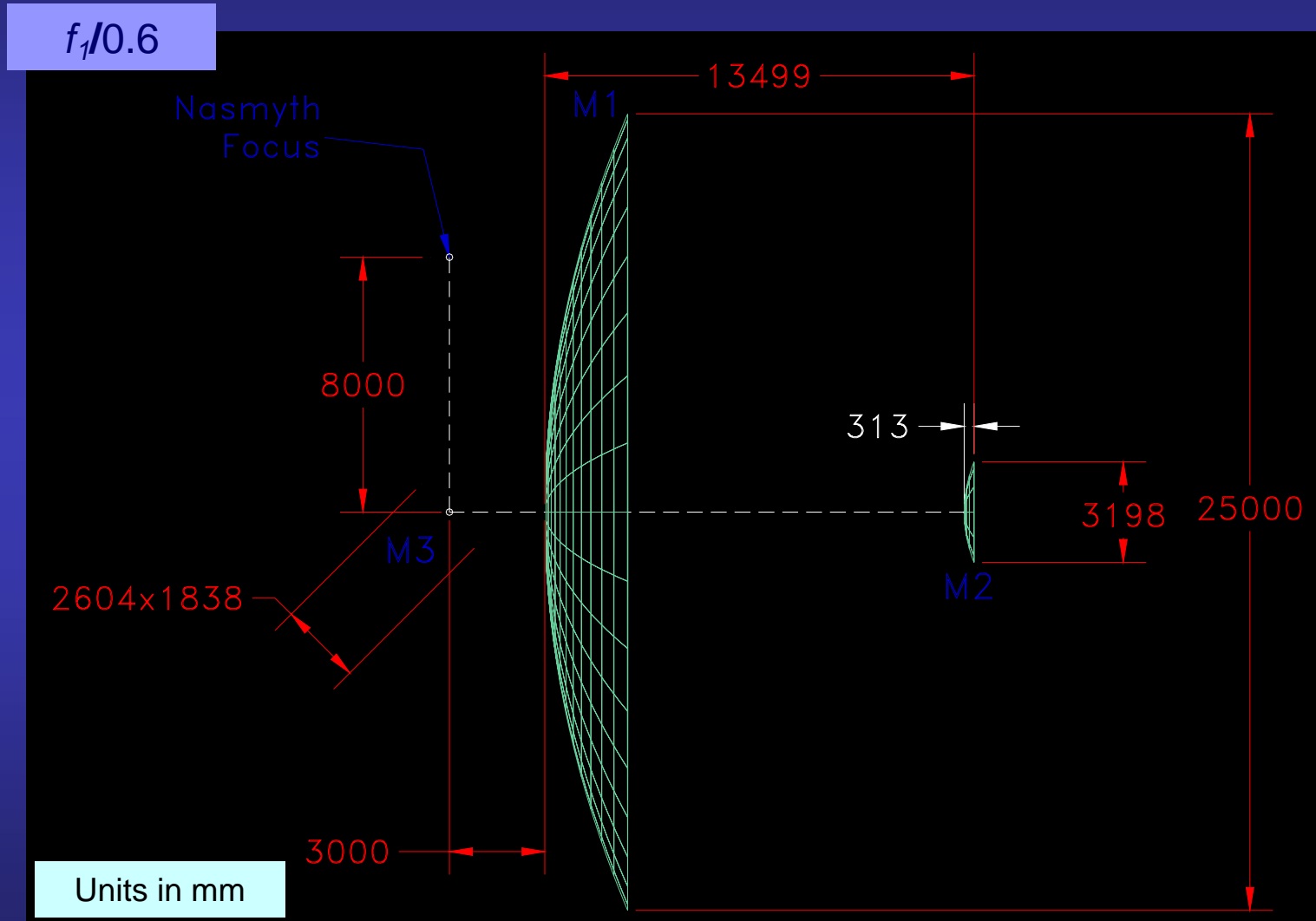
### M2

Diameter (with FOV provisions)  
Eccentricity  
Vertex Radius of Curvature  
Edge Angle from Secondary Focus

$D_2$	3.20	2.62	[m]
$\varepsilon_2$	1.169098	1.108191	
$R_{C2}$	3.922	2.105	[m]
$\theta_2$	3.58	3.58	[deg]

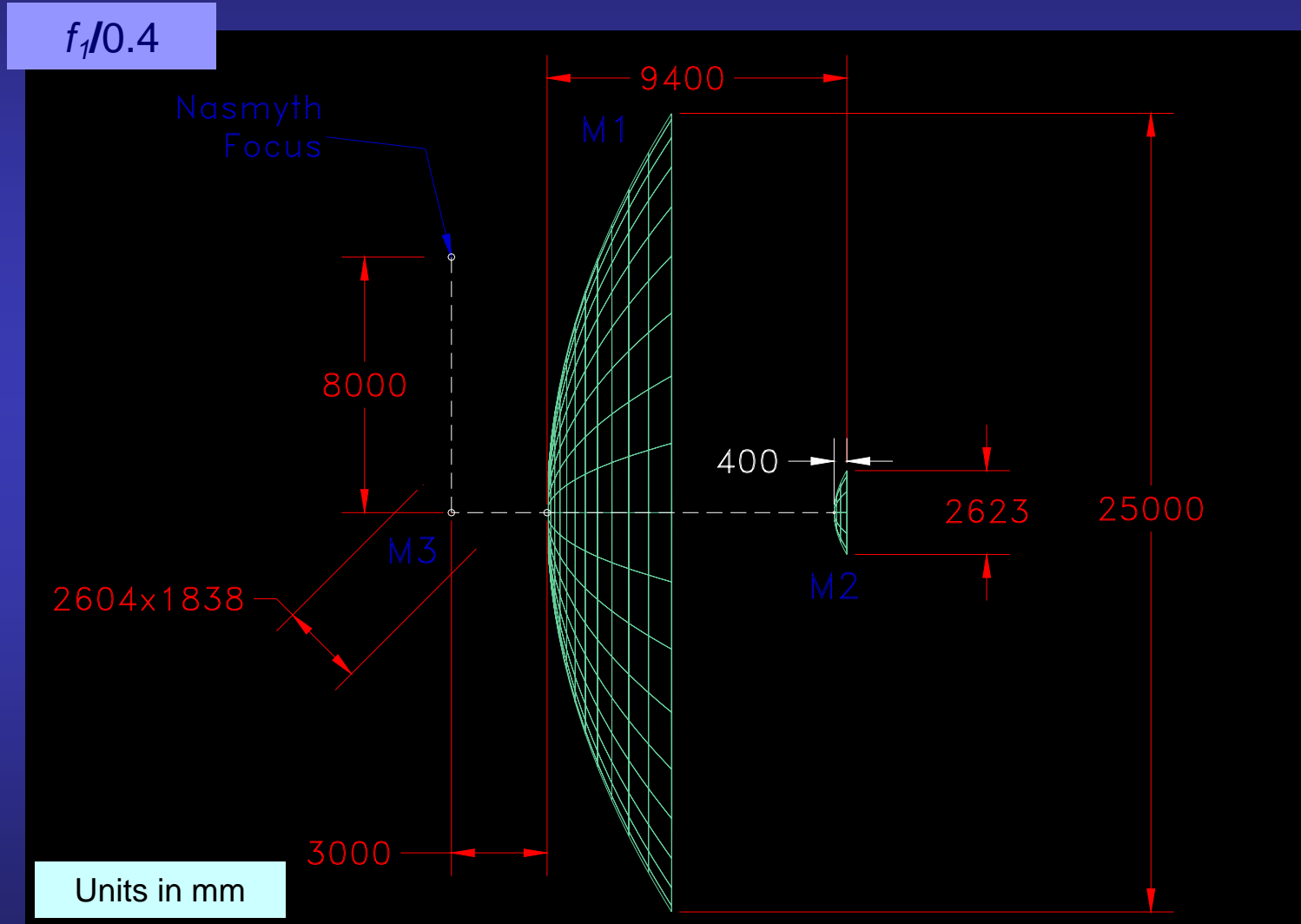
# Ritchey-Chrétien Optical Layout

$f_1/0.6$  vs.  $f_1/0.4$



# Ritchey-Chrétien Optical Layout

$f_1/0.6$  vs.  $f_1/0.4$

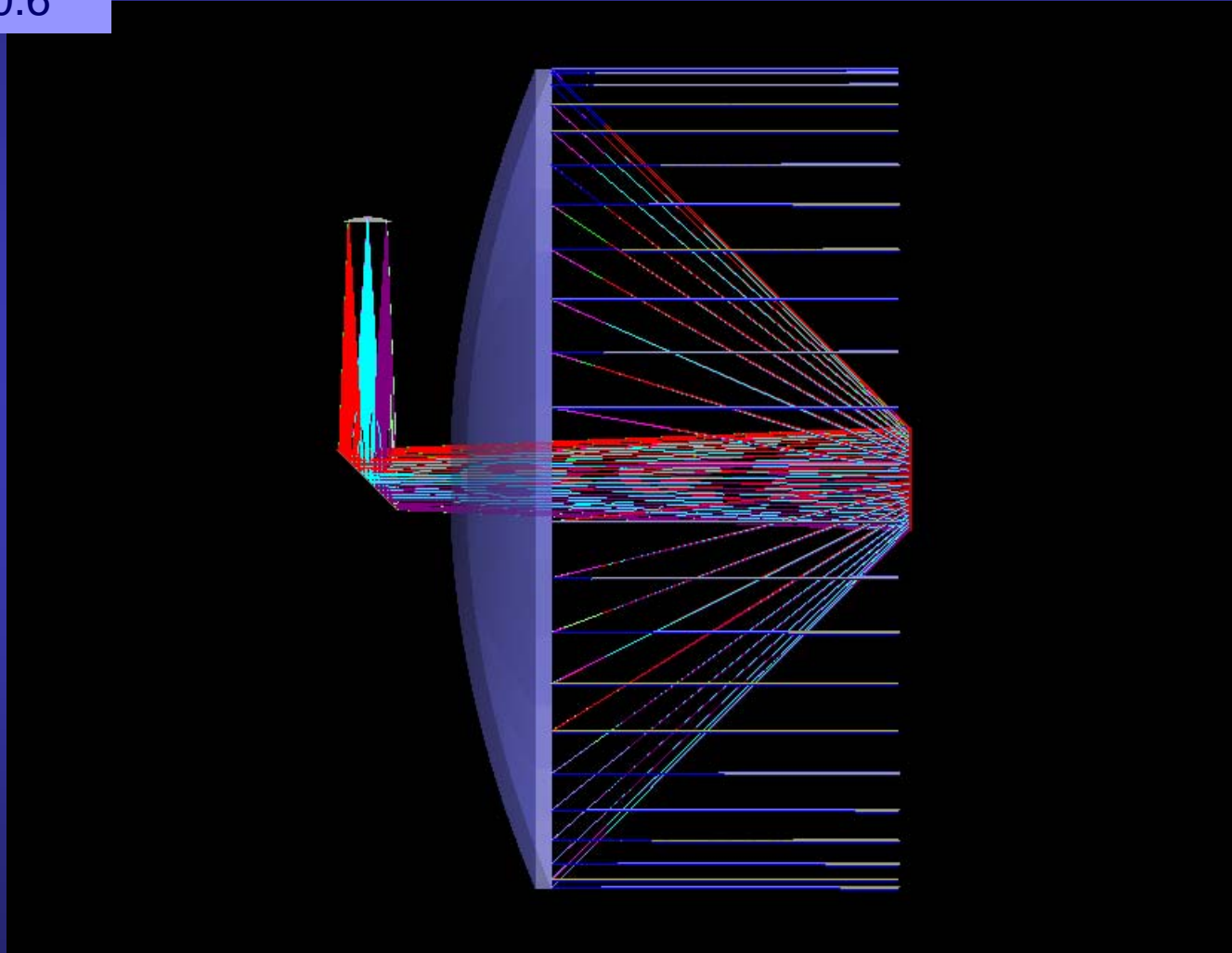


# Ritchey-Chrétien Optical Layout

$f_1/0.6$  vs.  $f_1/0.4$



$f_1/0.6$

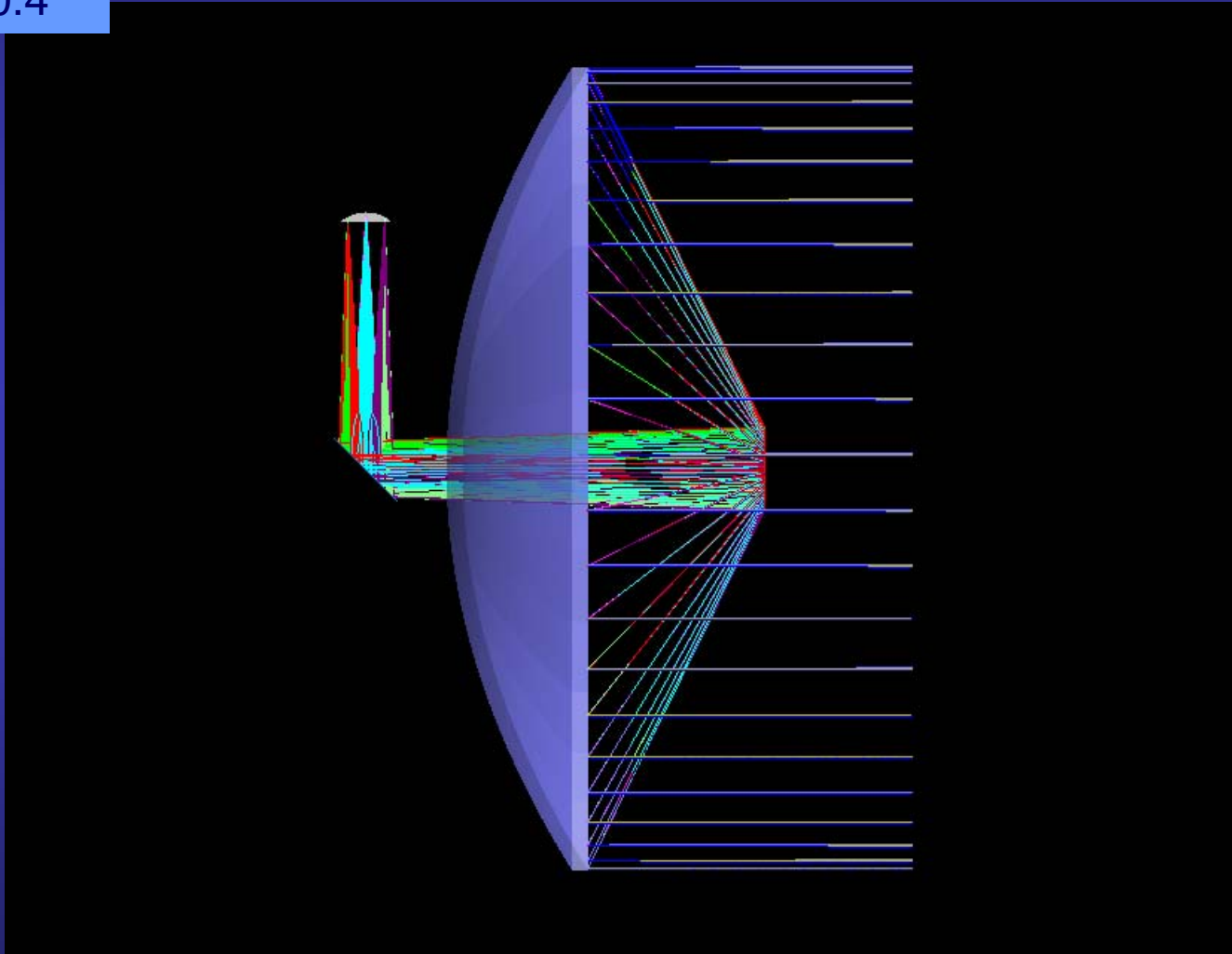


# Ritchey-Chrétien Optical Layout

$f_1/0.6$  vs.  $f_1/0.4$

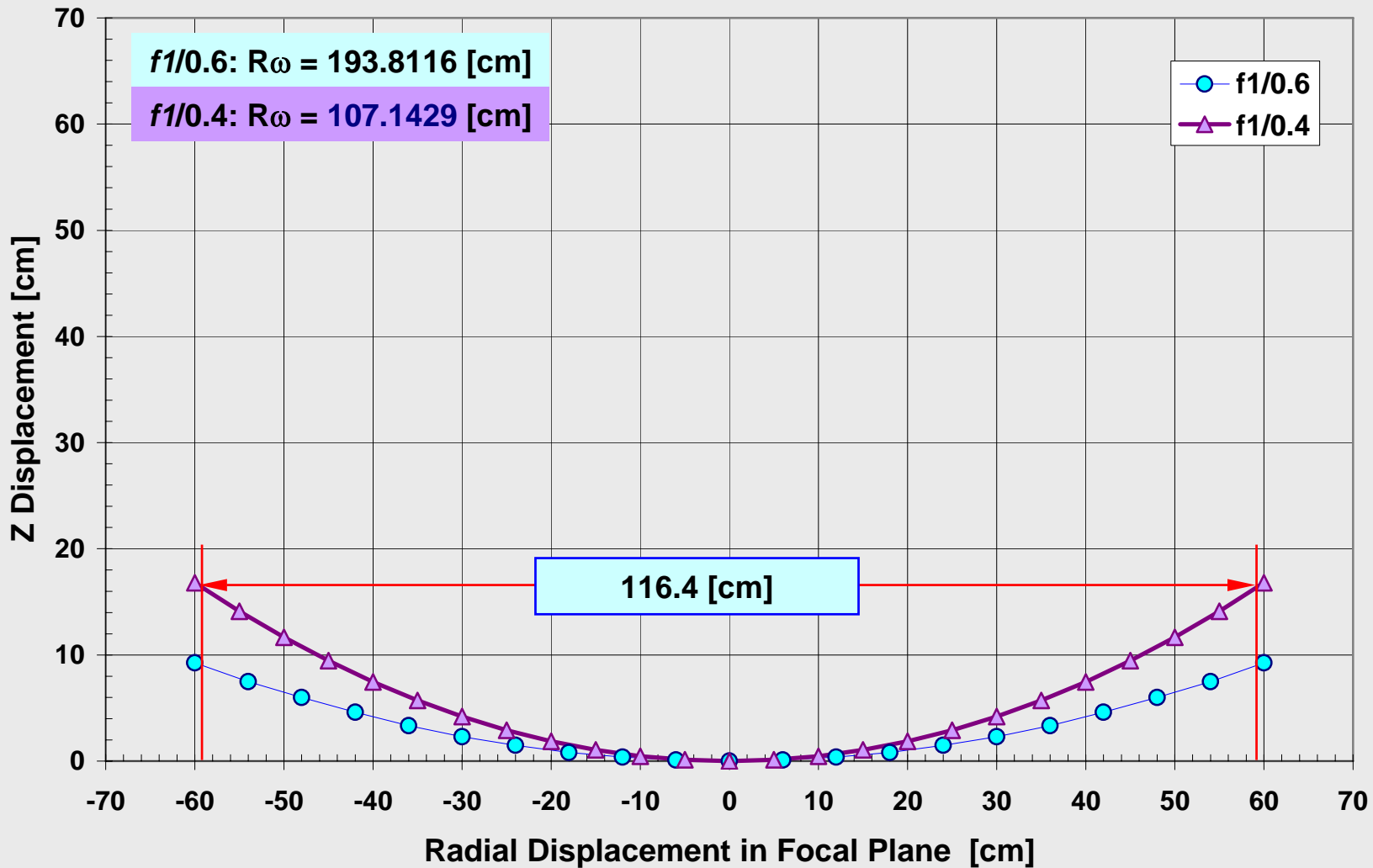


$f_1/0.4$



# FOV: Optimum Focal Surface Geometry

$f_1/0.6$  vs.  $f_1/0.4$



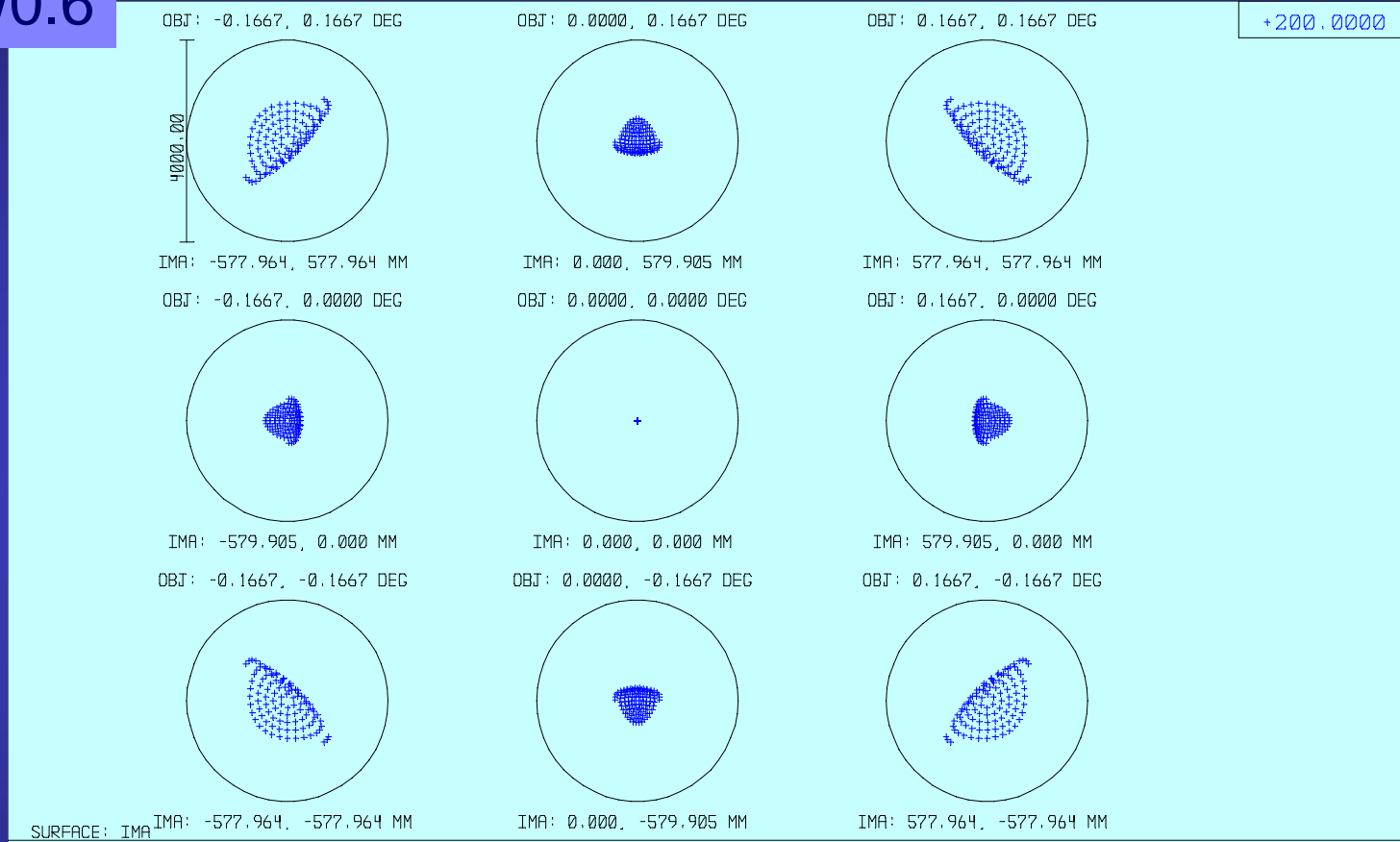


# FOV: Spot Diagram



$f_1/0.6$

$f_1/0.6$  vs.  $f_1/0.4$



## SPOT DIAGRAM

CCAT F1/0.6										
SAT JUL 14 2007      UNITS ARE $\mu\text{m}$ .										
FIELD :	1	2	3	4	5	6	7	8	9	
RMS RADIUS :	616.950	290.239	616.950	290.239	1.588	290.239	611.381	290.239	611.381	
GEO RADIUS :	1105.97	444.880	1105.97	444.880	2.765	444.880	1105.97	444.880	1105.97	
CIRCLE DIAM:	4000									
REFERENCE : CHIEF RAY										

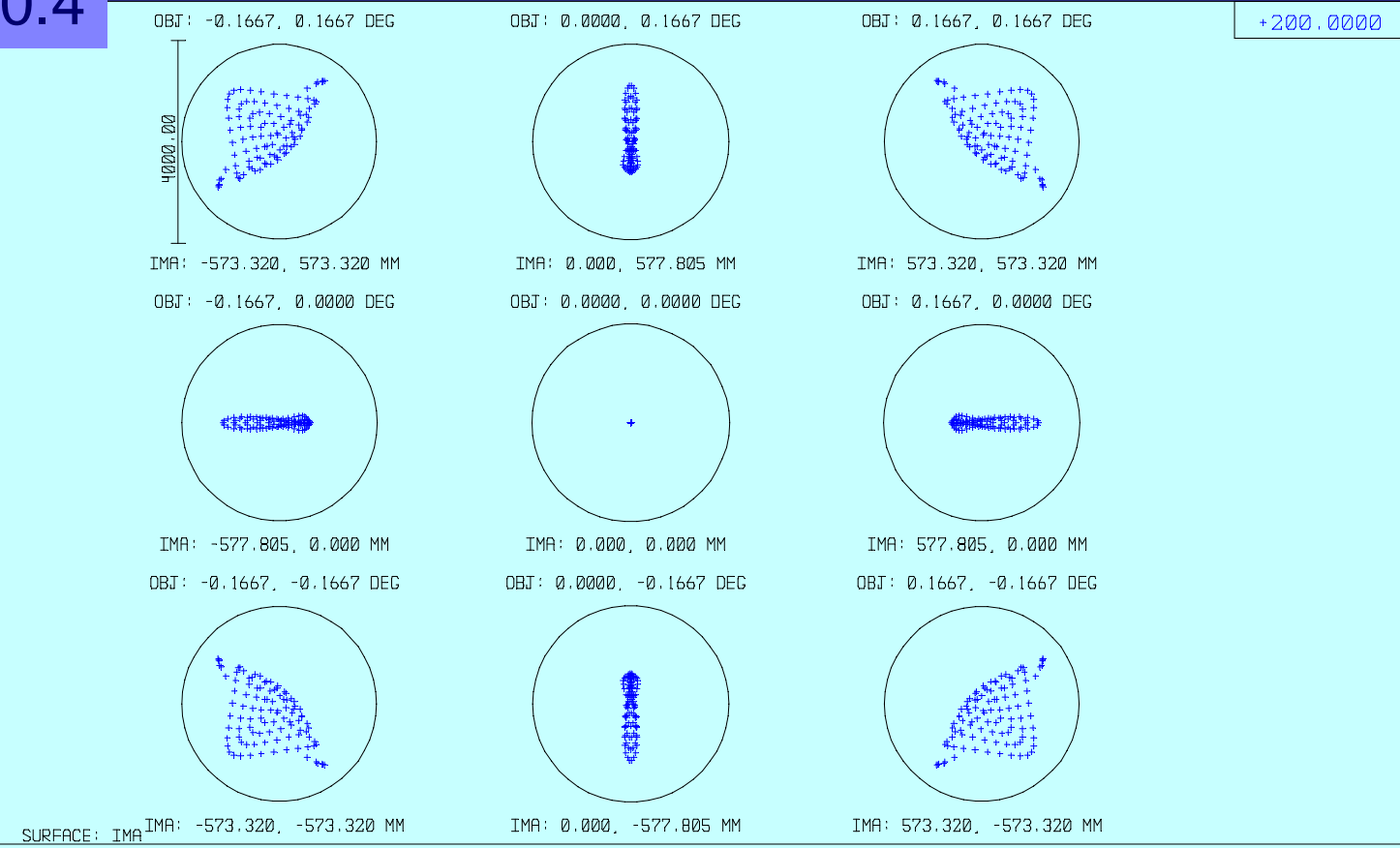
NAIC CORNELL UNIVERSITY  
LWCAM  
GERMAN CORTES MEDELLIN  
CCAT\_F1\_06.ZMX  
CONFIGURATION 1 OF 1

# FOV: Spot Diagram

## $f_1/0.6$ vs. $f_1/0.4$

$f_1/0.4$

+200.0000



### SPOT DIAGRAM

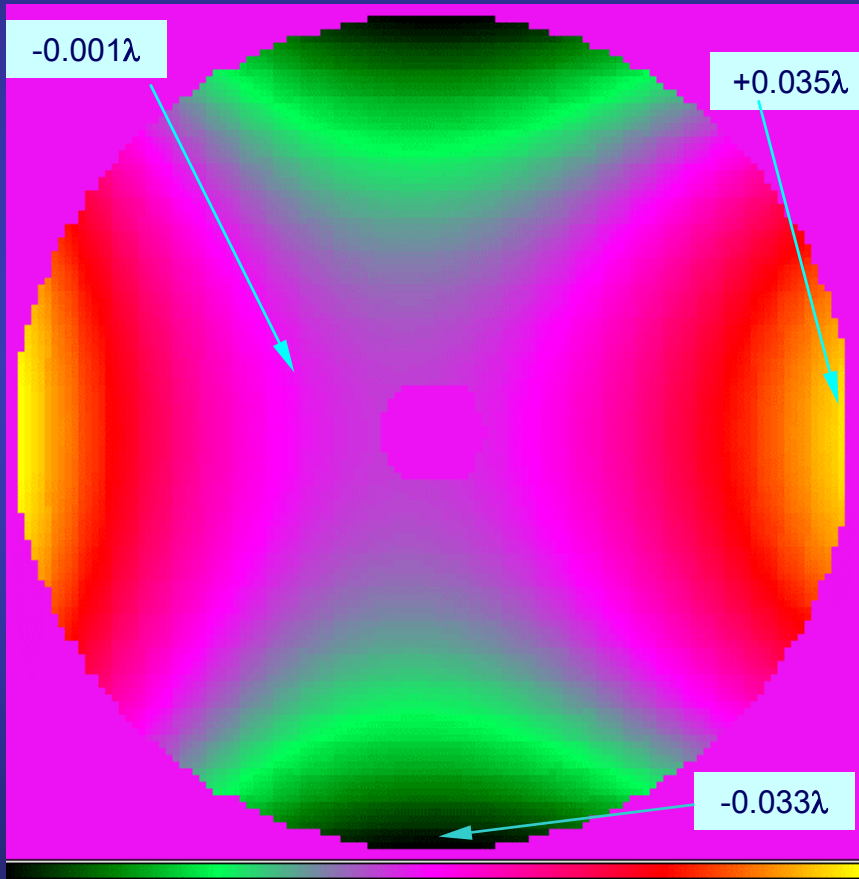
CCAT F1/0.4 + F/8										
SAT JUL 14 2007 UNITS ARE $\mu\text{m}$ . AIRY RADIUS : 1952 $\mu\text{m}$										
FIELD :	1	2	3	4	5	6	7	8	9	
RMS RADIUS :	848.662	501.937	848.662	501.937	1.121	501.937	848.662	501.937	848.662	
GEO RADIUS :	1503.45	1114.74	1503.45	1120.95	1.947	1120.95	1503.45	1114.74	1503.45	
SCALE BAR :	4000									
					REFERENCE : CHIEF RAY					

NAIC CORNELL UNIVERSITY  
 LWCAM  
 GERMAN CORTES MEDELLIN  
 CCAT\_F1\_04\_B.ZMX  
 CONFIGURATION 1 OF 1

# $f_1/0.6$ Uniform Illumination (at $200\ \mu\text{m}$ )



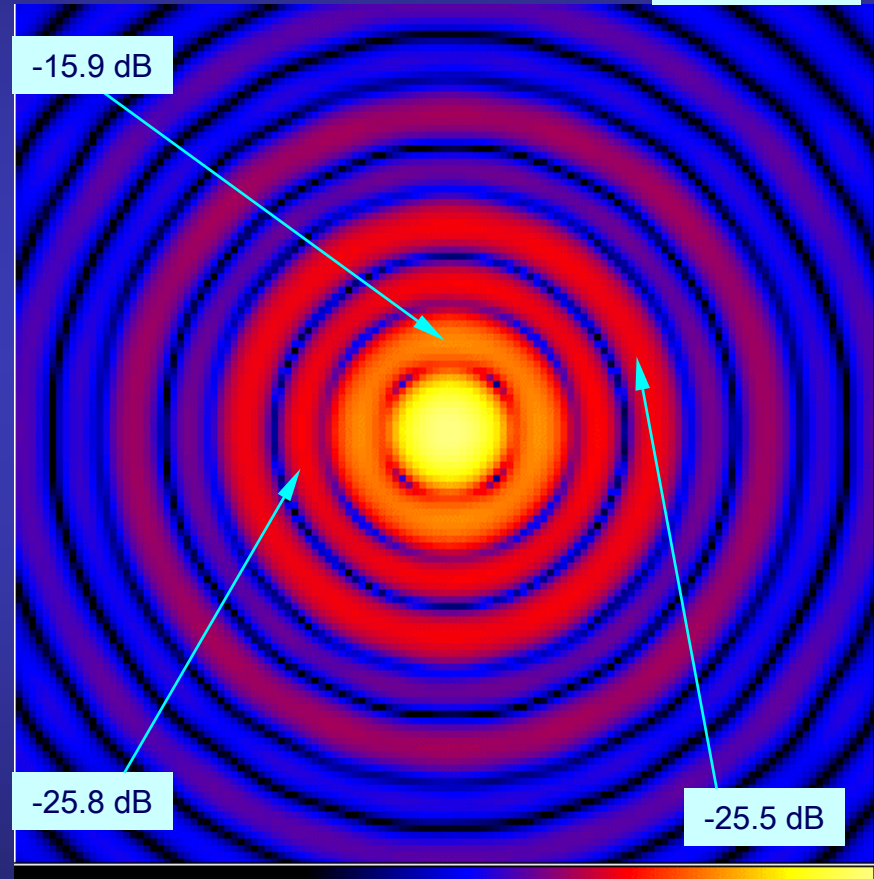
Strehl=96.8%  $\epsilon_{\text{rms}} = 0.0331\lambda = 6.6\ \mu\text{m}$



Phase Distribution at Aperture [ $\lambda$ ]

Beam=1.89"

51"x51"



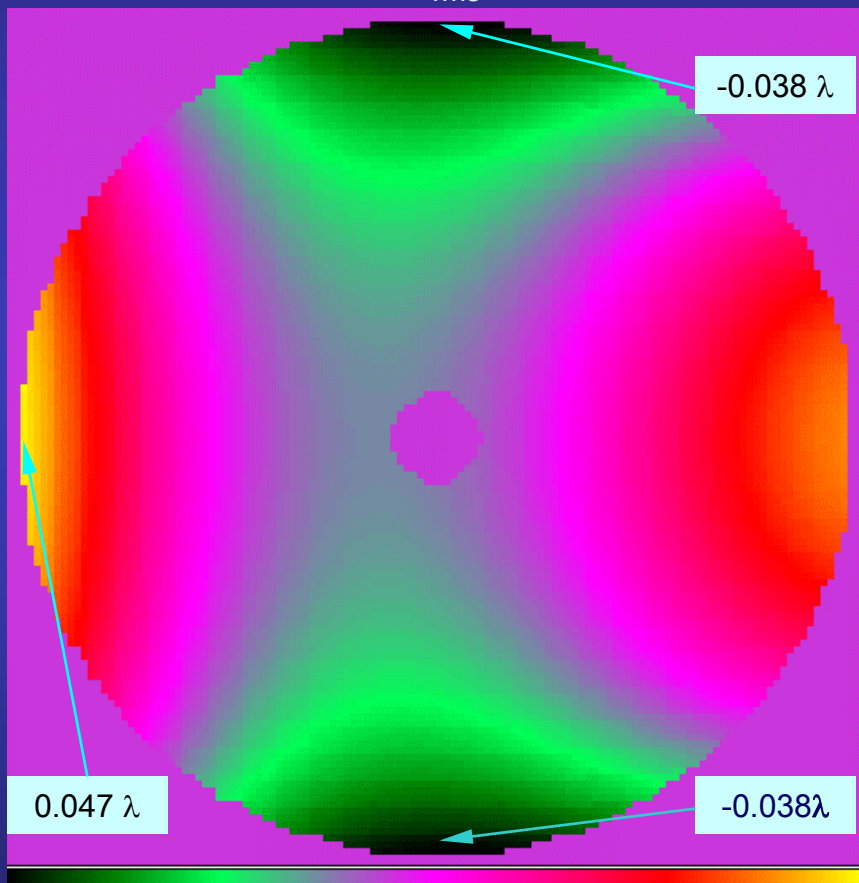
Far Field Radiation Pattern [dB]

# $f_1/0.4$ Uniform Illumination (at $200\ \mu\text{m}$ )



Strehl=95.0%

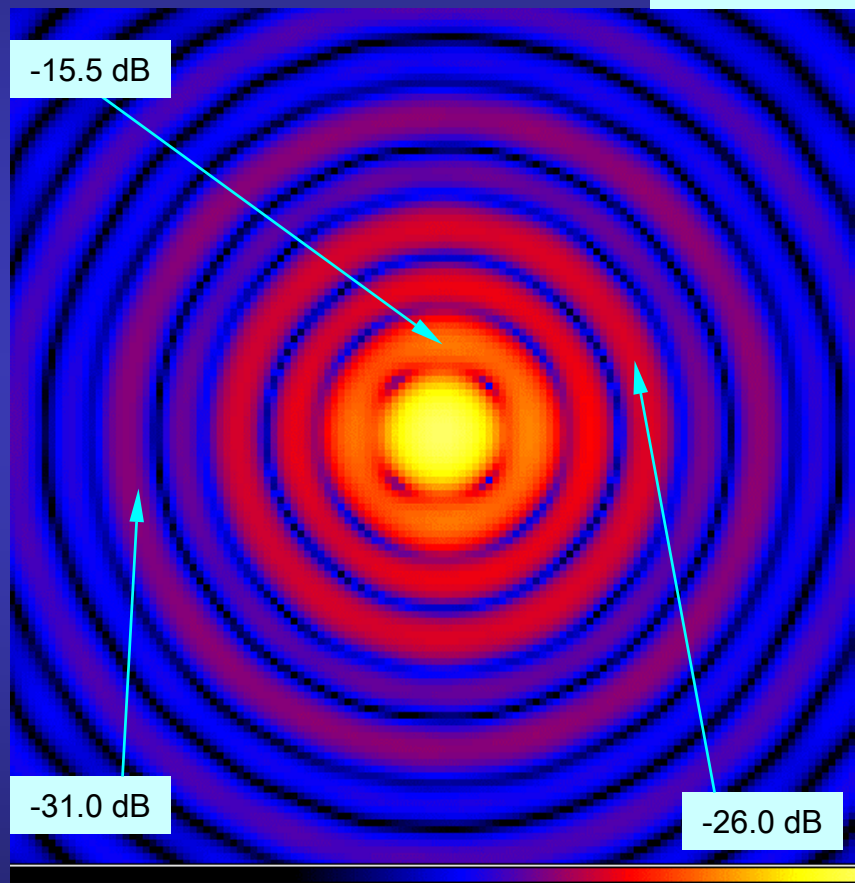
$\epsilon_{\text{rms}} = 0.0358\lambda = 7.2\ \mu\text{m}$



Phase Distribution at Aperture [ $\lambda$ ]

Beam=1.89"

51"x51"



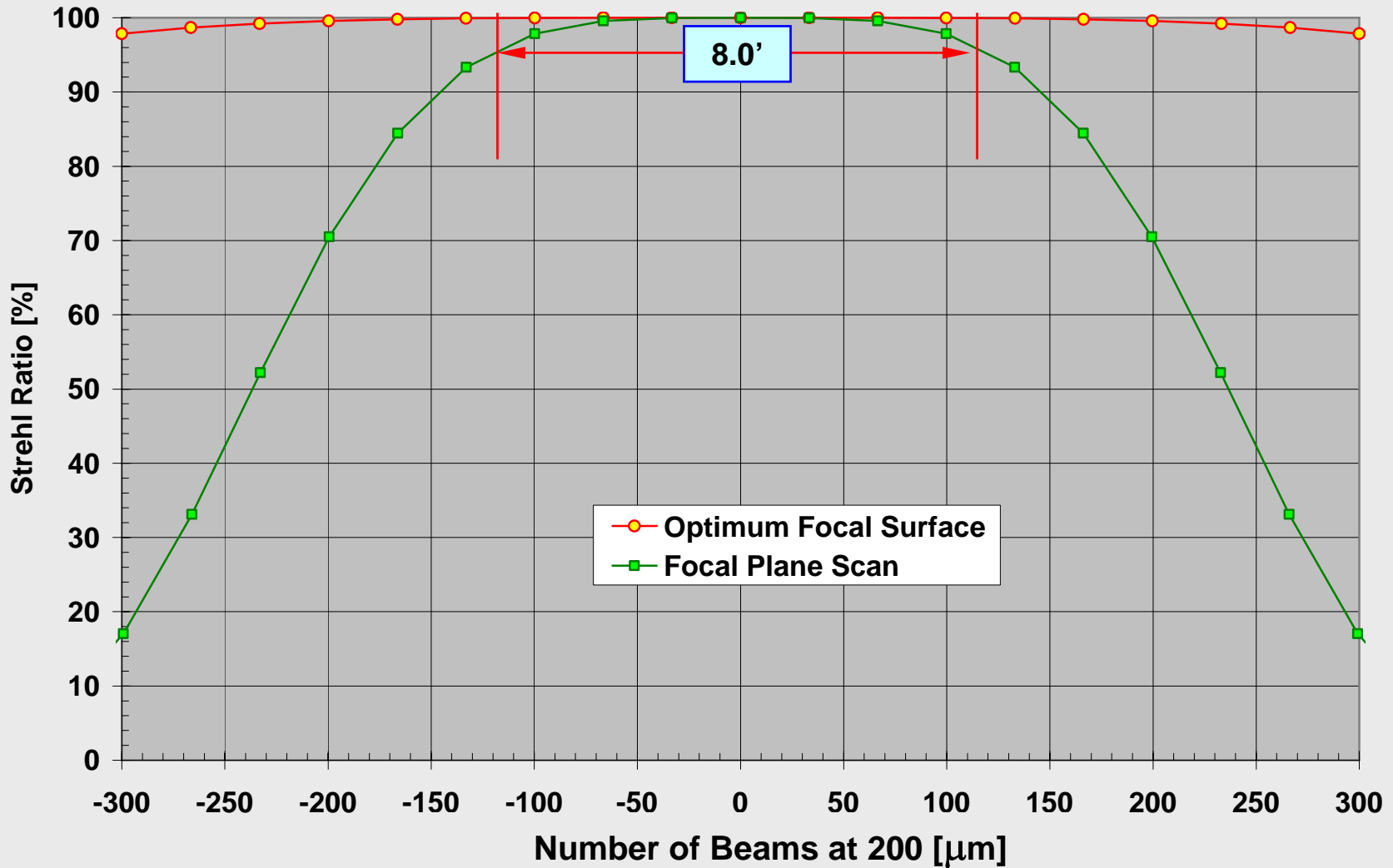
Far Field Radiation Pattern [dB]

# Strehl Ratio vs. Number of Beams

$f_1/0.6$  vs.  $f_1/0.4$



$f_1/0.6$



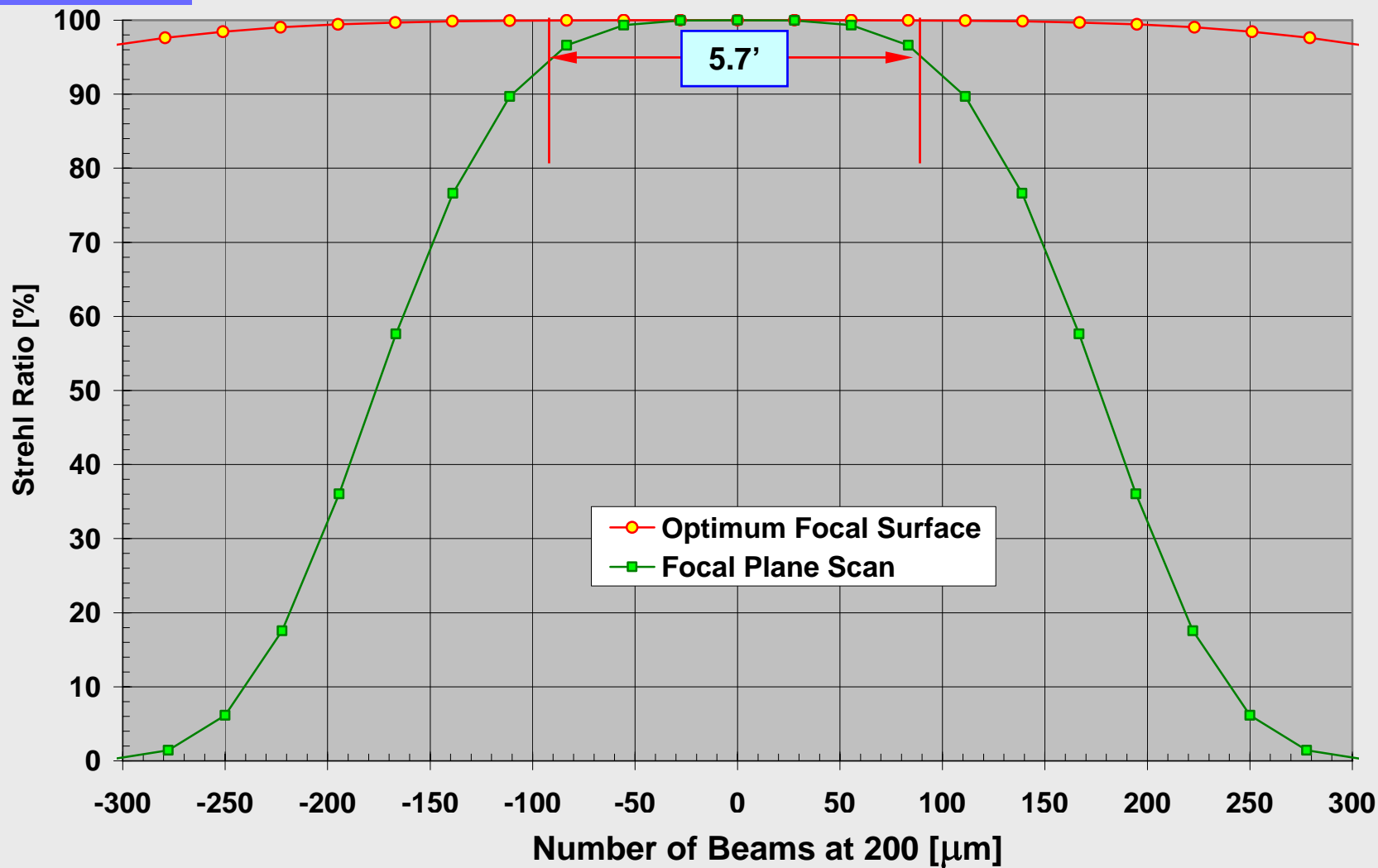
# Strehl Ratio vs. Number of Beams

$f_1/0.6$  vs.  $f_1/0.4$



CCAT

$f_1/0.4$

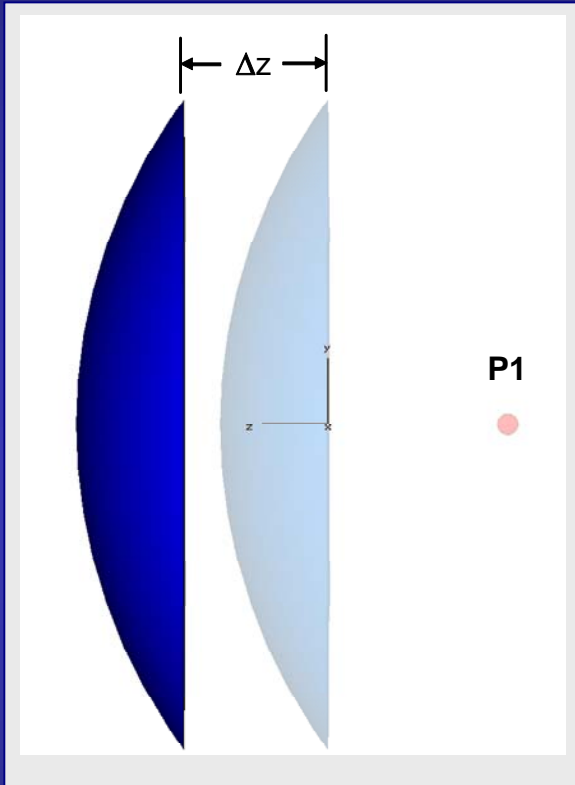




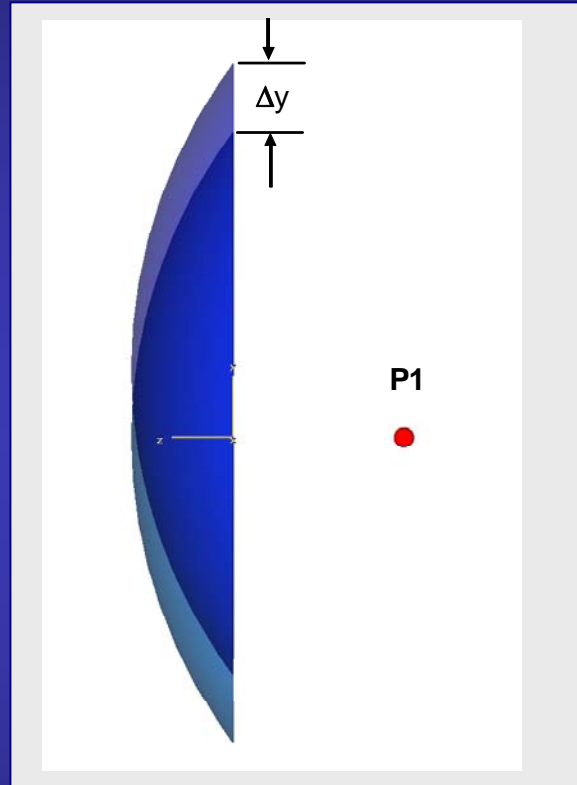
CCAT

# M2 Positioning and Image Quality

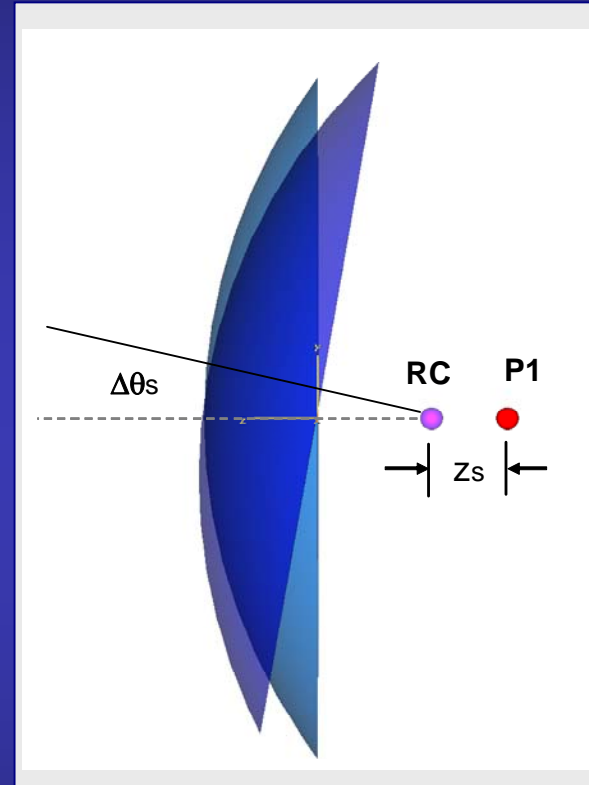
# M2 Positioning and Image Quality



**FOCUSING**



**DE-CENTER**



**TILT**

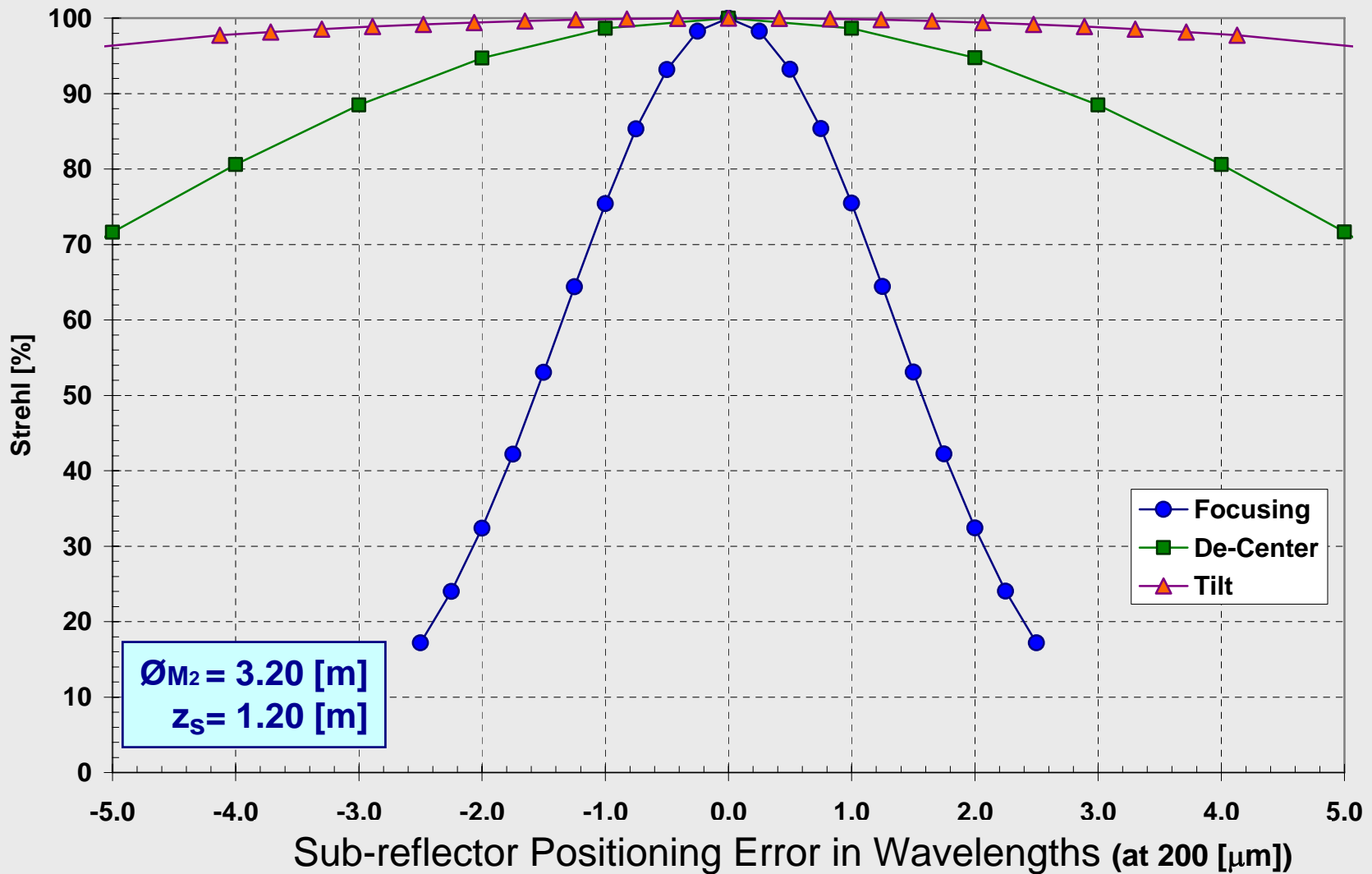


# Strehl Ratio vs. $M_2$ Positioning

$f_1/0.6$  vs.  $f_1/0.4$



$f_1/0.6$

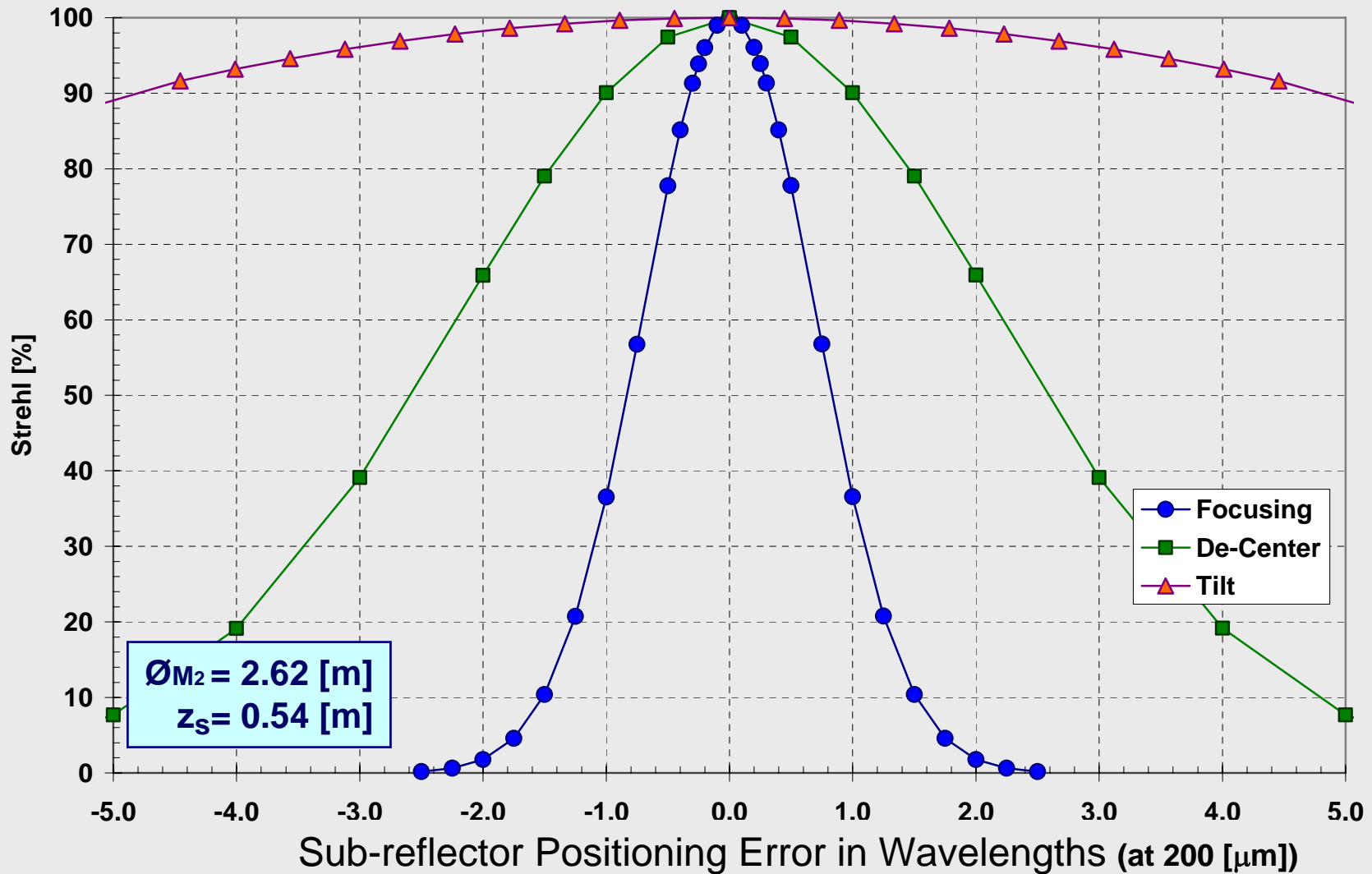


# Strehl Ratio vs. $M_2$ Positioning

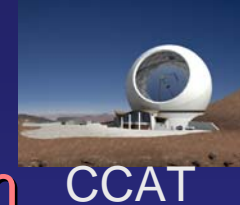
$f_1/0.6$  vs.  $f_1/0.4$



$f_1/0.4$



# M<sub>2</sub> Positioning Requirements for Image Quality Strehl > 95% at 200 μm



	Focus $ \Delta z $ [μm]	De-center $ \Delta x^2 + \Delta y^2 ^{1/2}$ [μm]	Diameter $\varnothing_{M_2}$ [m]
$f_1/0.6$	< 80.0	< 380.0	3.20
$f_1/0.4$	< 45.0	< 120.0	2.62



# M<sub>2</sub> Positioning and Beam Deviation

# Beam Deviation vs. $M_2$ Lateral Displacement

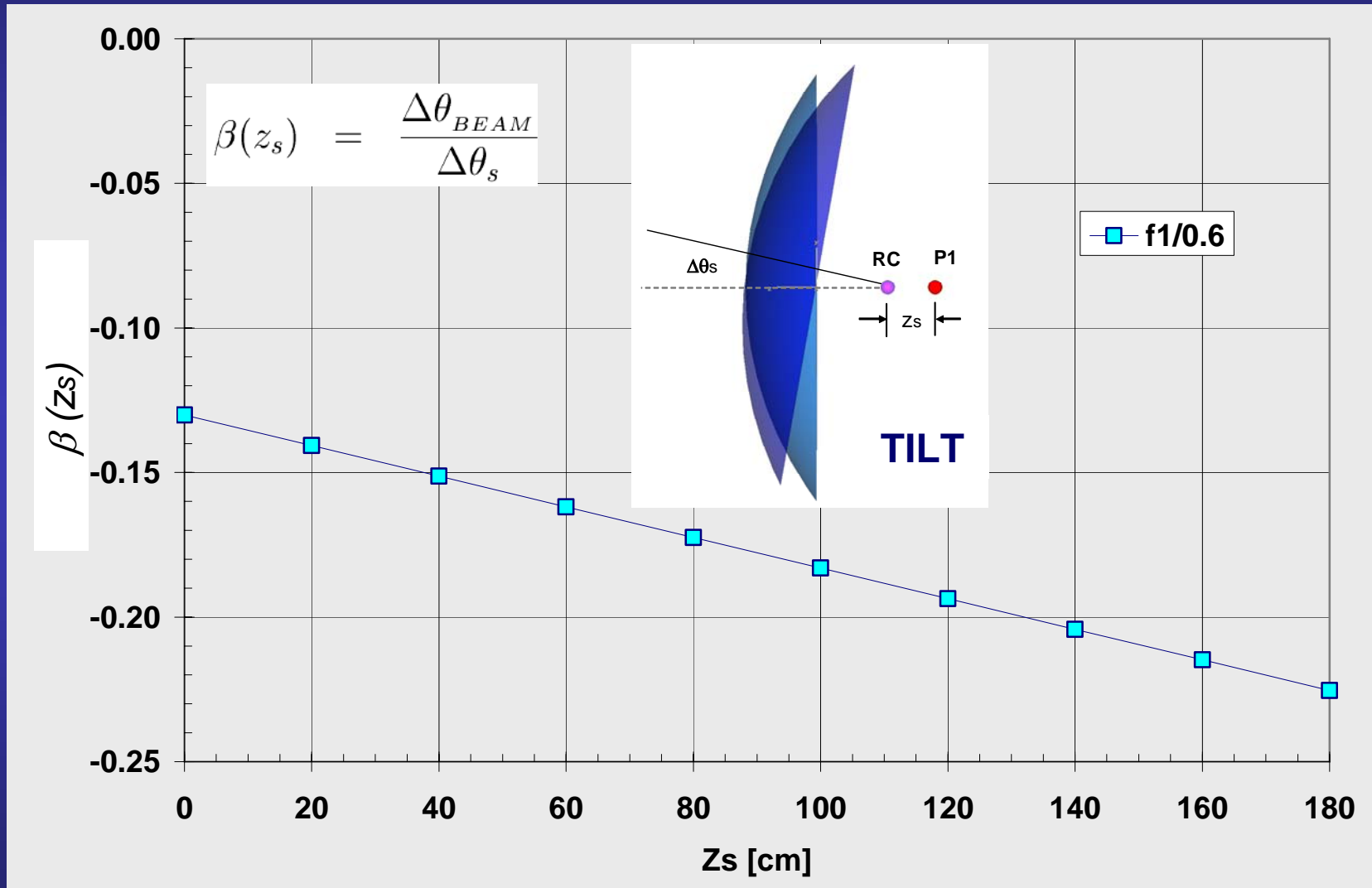


$f_1/0.6$  vs.  $f_1/0.4$  at 200  $\mu\text{m}$

	Lateral Sensitivity [arcsec/mm]	Diameter $\text{\O}M_2$ [m]
$f_1/0.6$	-10.93	3.20
$f_1/0.4$	-14.33	2.62

# Beam Deviation vs. $M_2$ Tilt

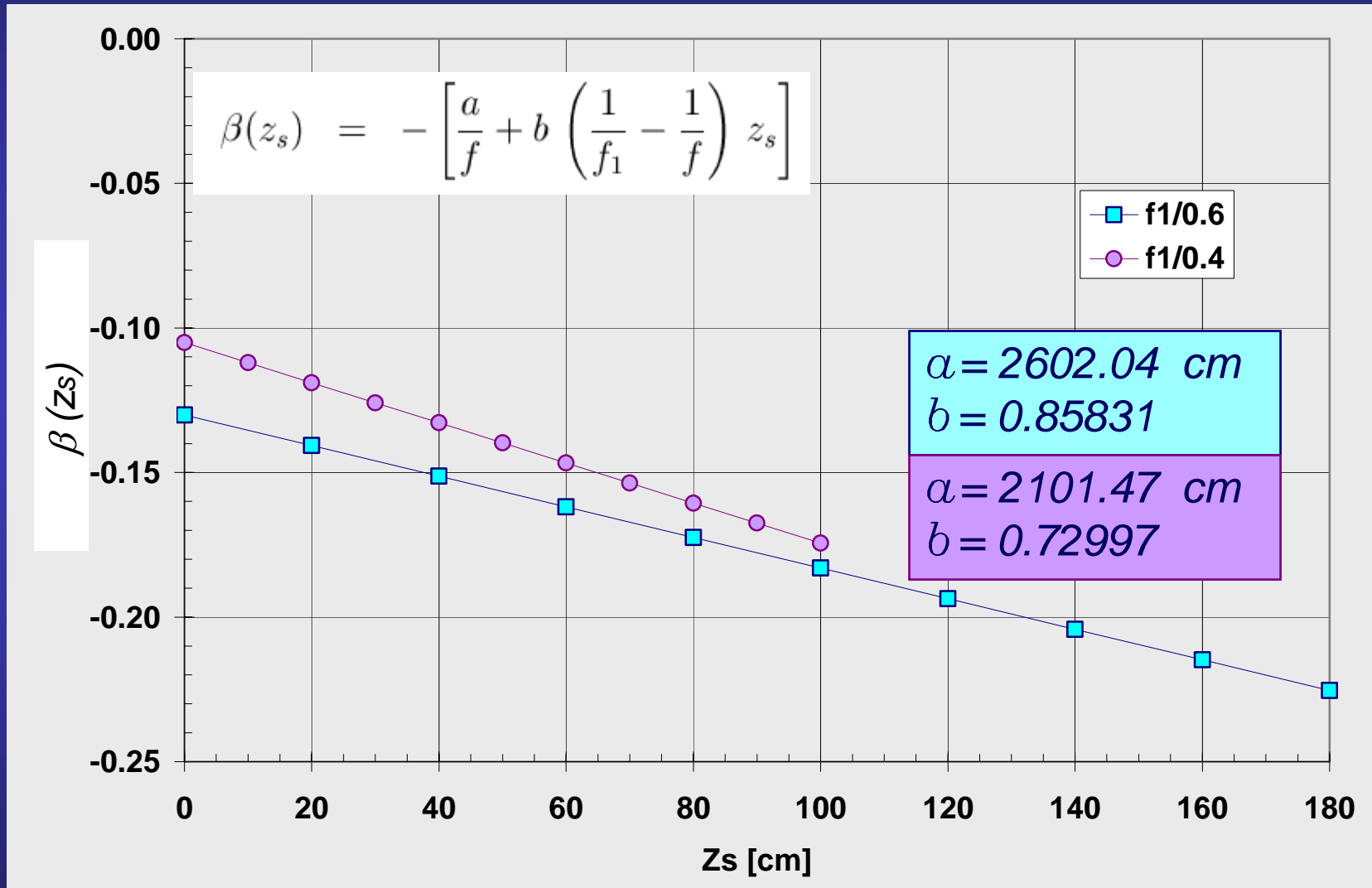
$f_1/0.6$  vs.  $f_1/0.4$



at 200  $\mu\text{m}$

# Beam Deviation vs. $M_2$ Tilt

$f_1/0.6$  vs.  $f_1/0.4$



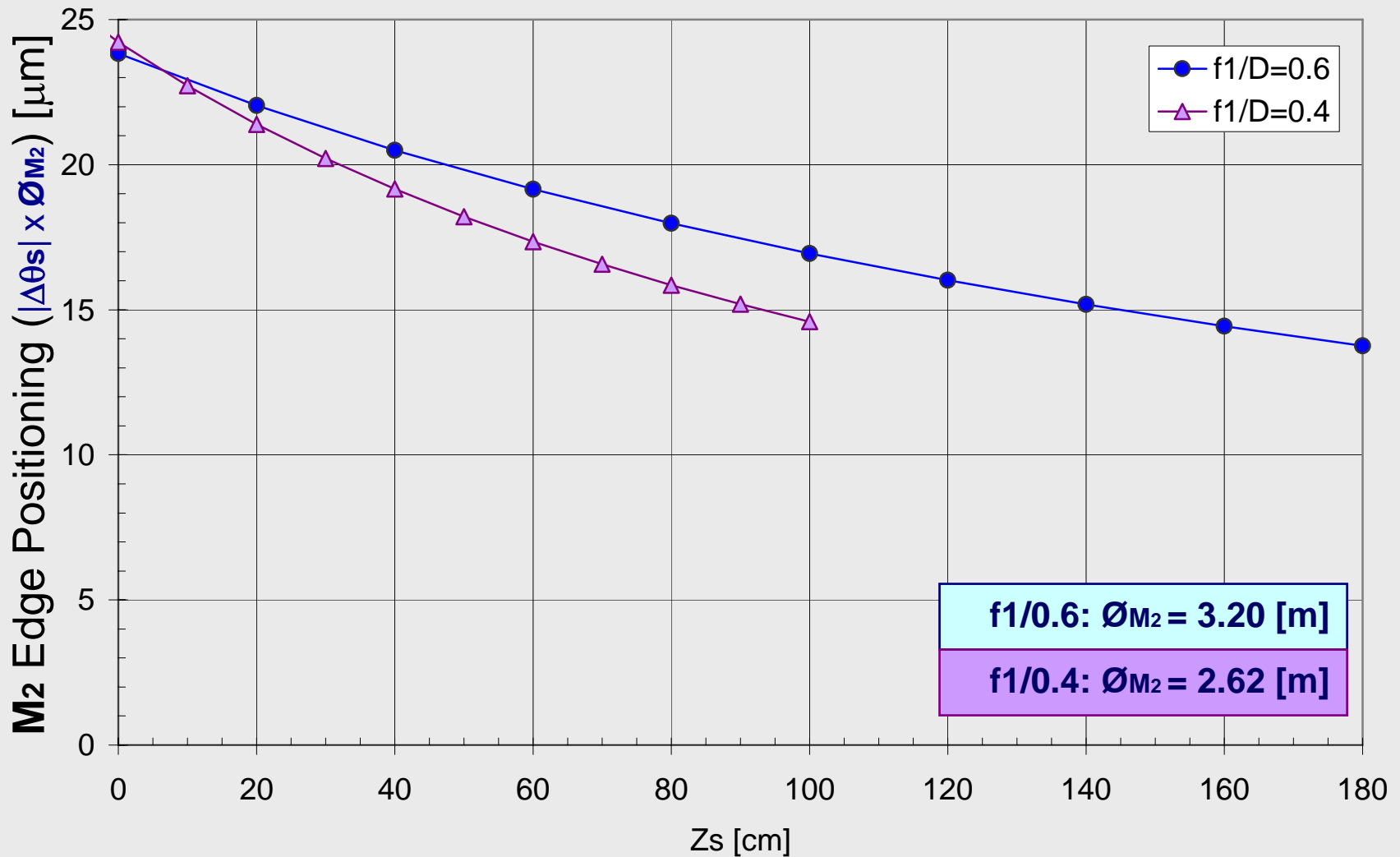
at 200 [ $\mu$ m]

# M<sub>2</sub> Positioning Requirements for Pointing

$f_1/0.6$  vs.  $f_1/0.4$



HPBW/10 at 200  $\mu\text{m}$



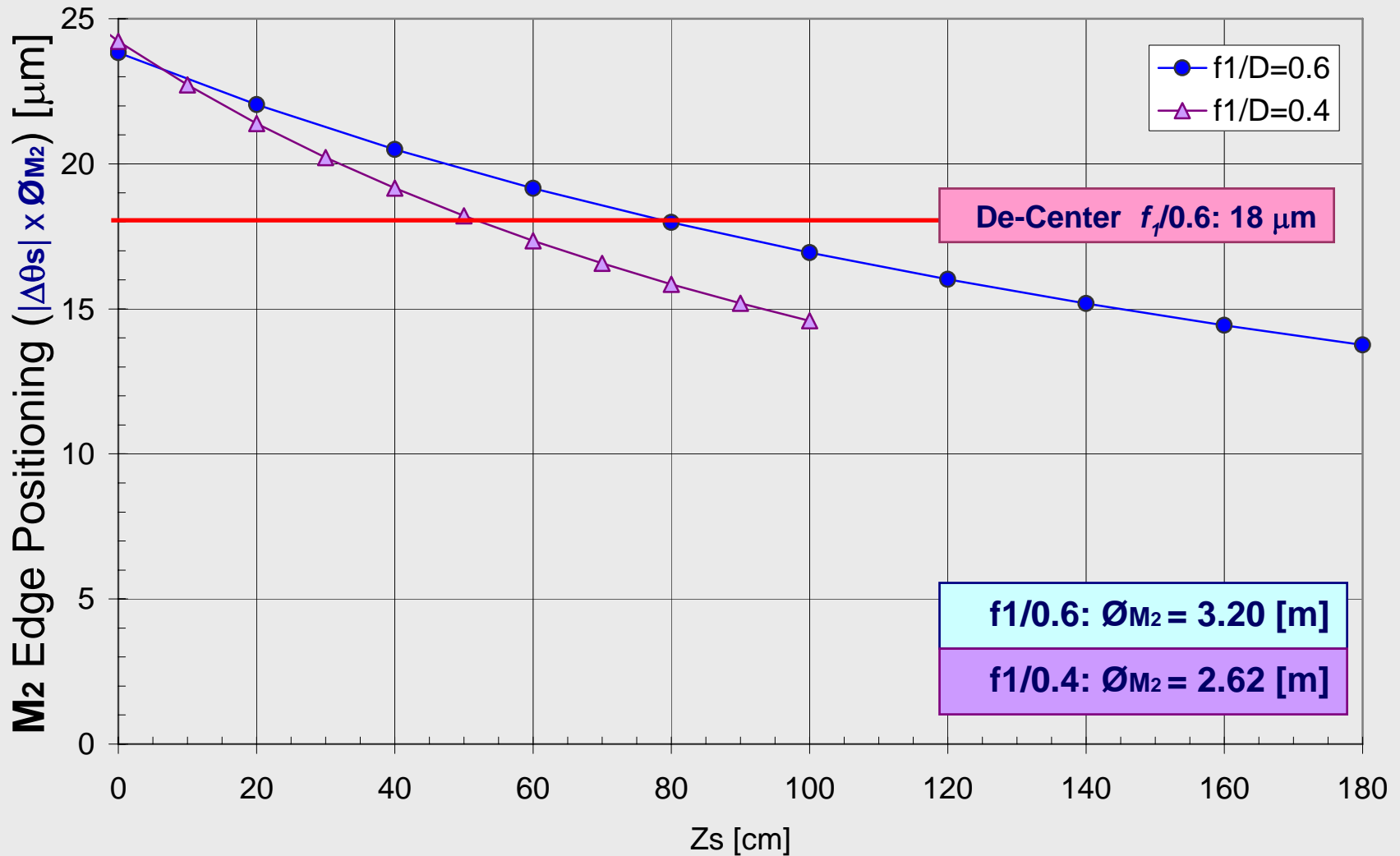


# M<sub>2</sub> Positioning Requirements for Pointing

$f_1/0.6$  vs.  $f_1/0.4$



HPBW/10 at 200  $\mu\text{m}$

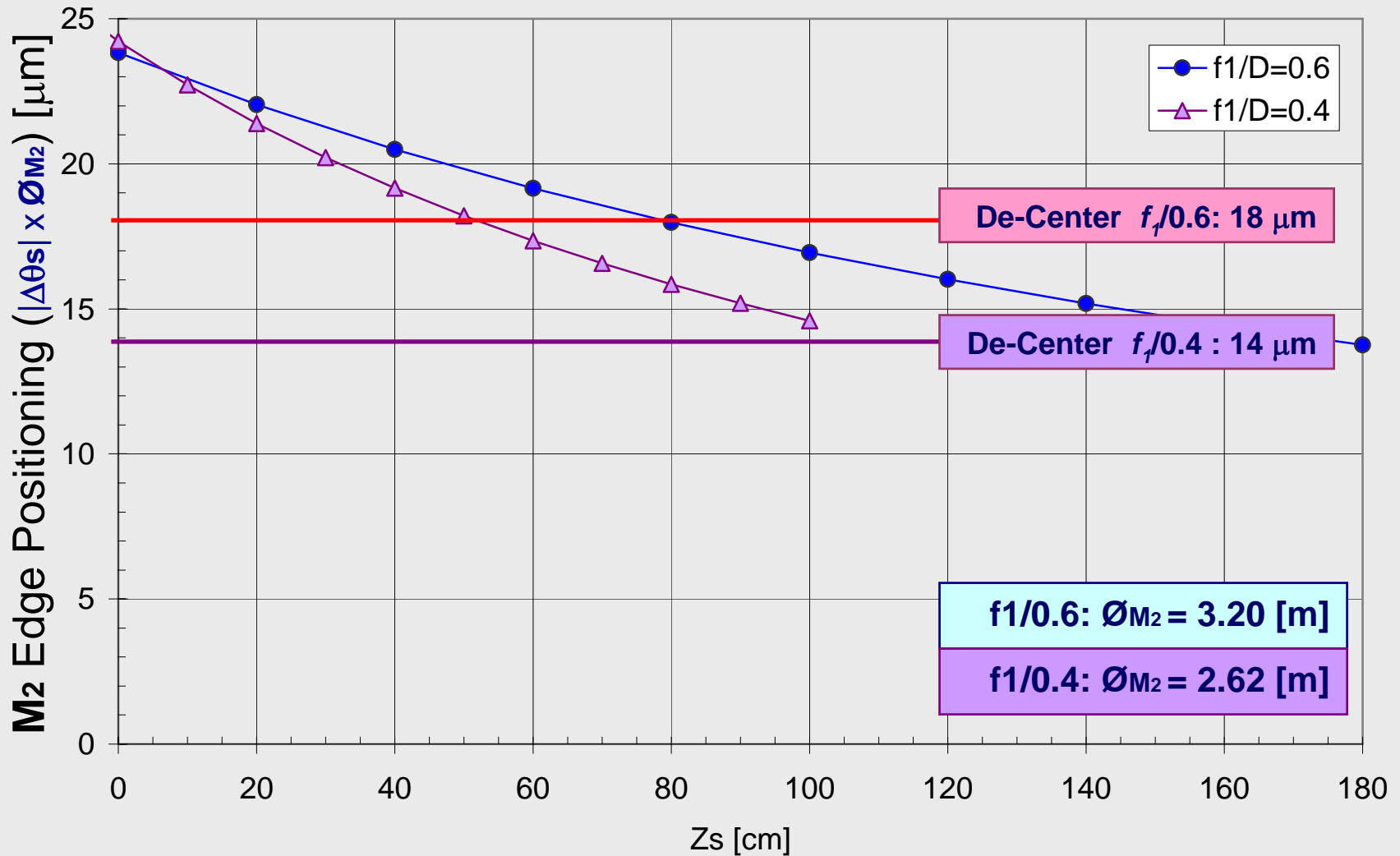


# M<sub>2</sub> Positioning Requirements for Pointing

$f_1/0.6$  vs.  $f_1/0.4$



HPBW/10 at 200  $\mu\text{m}$





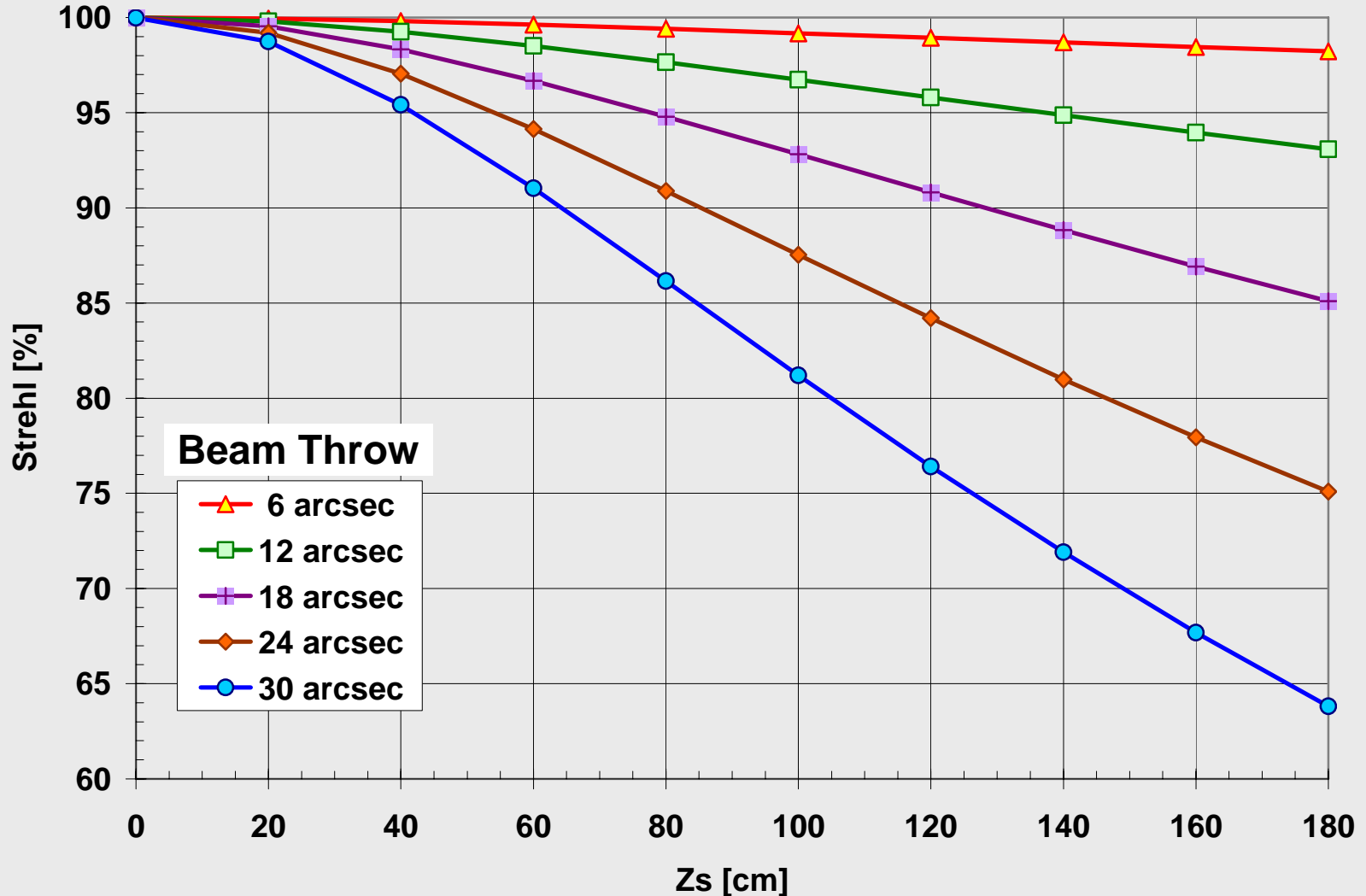
# M<sub>2</sub> Nutation and Image Quality

# M<sub>2</sub> Nutation and Image Quality

$f_1/0.6$  vs.  $f_1/0.4$



$f_1/0.6$



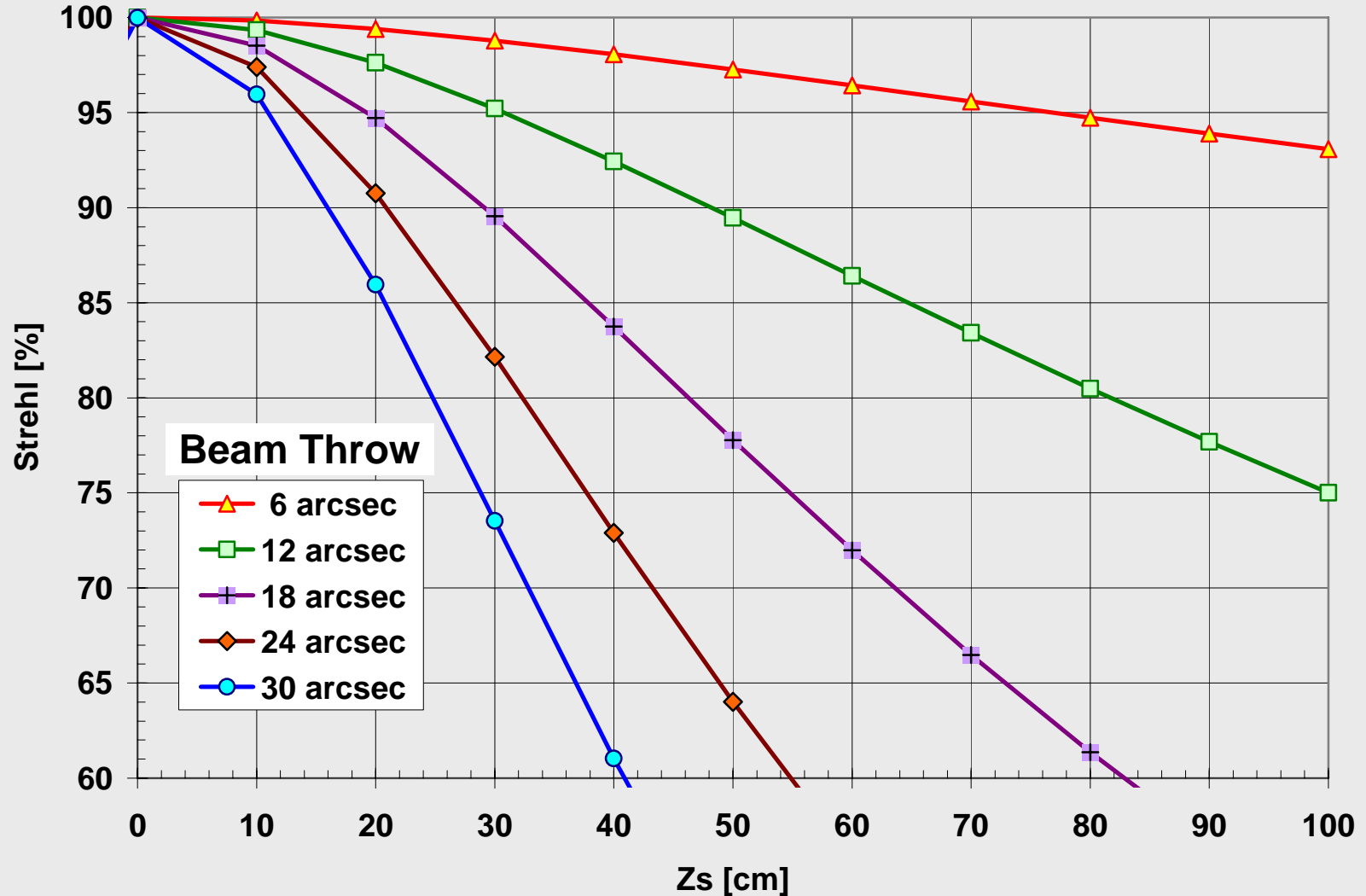
$\lambda = 200 \mu\text{m}$

# M<sub>2</sub> Nutation and Image Quality

$f_1/0.6$  vs.  $f_1/0.4$



$f_1/0.4$



$\lambda = 200 \mu\text{m}$

# Conclusions I



- ◆ There is reduction in the distance between the main reflector vertex and the edge of M2 from 13.5m with an f1/0.6 design to a 9.4m with a f1/0.4 design.
- ◆ Reduction in M2 diameter:
  - for f1/0.6 design is 3.2m
  - for f1/0.4 design is 2.6m.
- ◆ The calculated **Strehl ratio variations** over the 20' FOV
  - for f1/0.6 design are better than 97% (optimal focal surface).
  - for f1/0.4 design are better than 95% (optimal focal surface).
- ◆ Size of FOV on a **flat** focal plane:
  - for f1/0.6 is 8.0 arcmin, with a Strehl  $\geq$  95%
  - for f1/0.4 is 5.7 arcmin, with a Strehl  $\geq$  95%
- ◆ Radius of curvature of the optimal focal surface at Nasmyth Foci
  - for f1/0.6 is 1.94m, and
  - for f1/0.4 is 1.07m.

# Conclusions I Cont...



- ◆ M2 Positioning and Image Quality at  $200\mu\text{m}$ :
  - Both cases are dominated by M2 focusing sensitivity, but while for the f1/0.6 it requires maintain the M2 focusing errors  $<80\mu\text{m}$ , for an f1/0.4 it requires  $<45\mu\text{m}$ , in order to maintain an  $\text{Strehl} \geq 95\%$ .
- ◆ M2 Positioning and Pointing requirement of  $\theta_{\text{HPFW}}/10$  at  $200\mu\text{m}$ :
  - For f1/0.6 it requires M2 edge-to-edge displacement due to tilts be between  $14\mu\text{m}$  and  $24\mu\text{m}$ , depending the location of the center of nutation. While M2 lateral displacements have to be  $< 18\mu\text{m}$ .
  - For f1/0.4 it requires M2 edge-to-edge displacement due to tilts be between  $14.5\mu\text{m}$  and  $24\mu\text{m}$ , depending the location of the center of nutation. While M2 lateral displacements have to be  $< 14\mu\text{m}$ .
- ◆ M2 Chopping:
  - Distance between M2 vertex and Prime Focus is almost half for f1/0.4 compared with f1/0.6, which for chopping kinematics and control purposes is better.
  - Number of beam throws with  $\text{Strehl} \geq 95\%$  is **8 beams** for f1/0.6 and **4 beams** for f1/0.4, when the center of nutation is located halfway between M2 vertex and prime focus



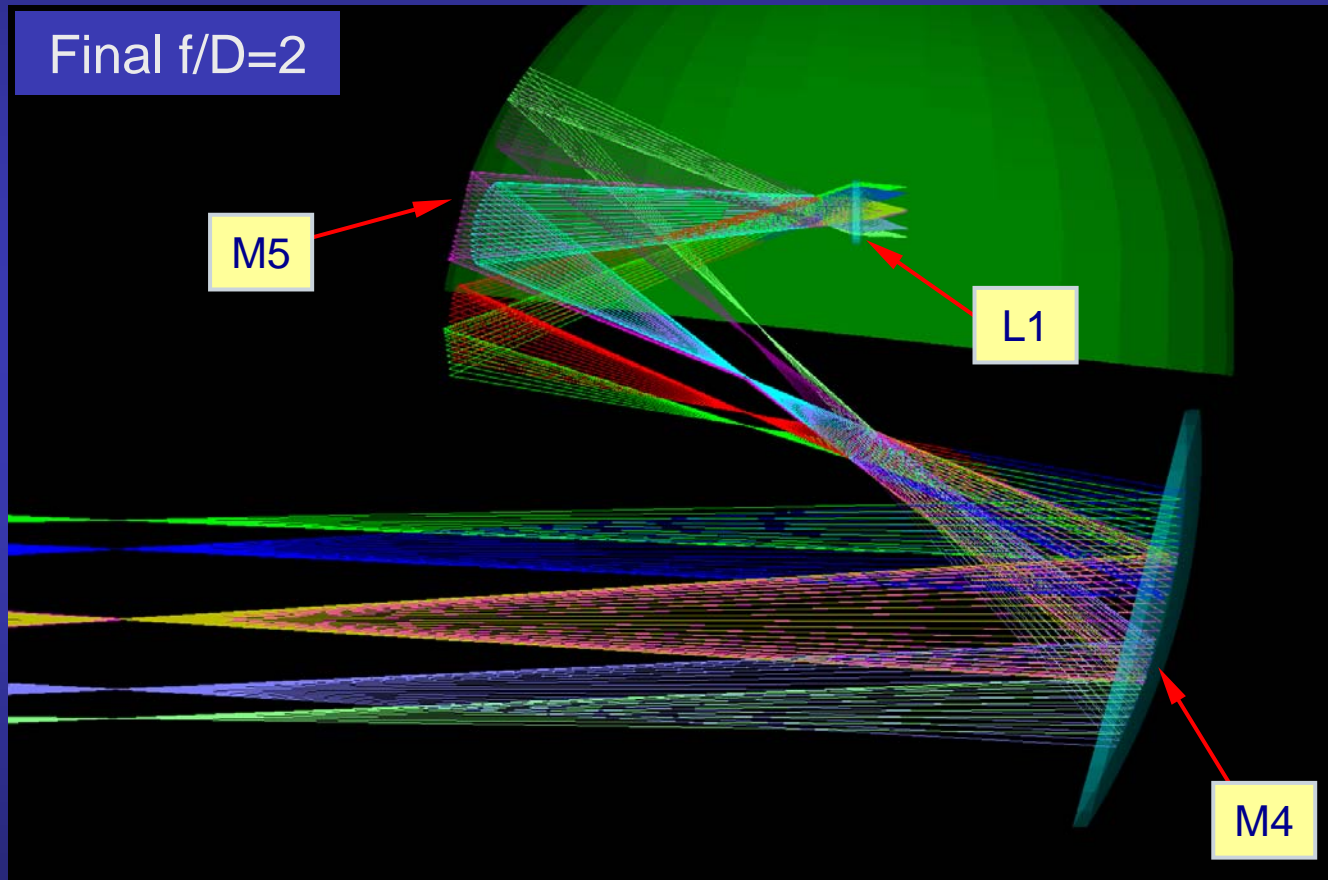
CCAT

# Re-Imaging Optics Impact



# LW-Cam Re-imaging Optics

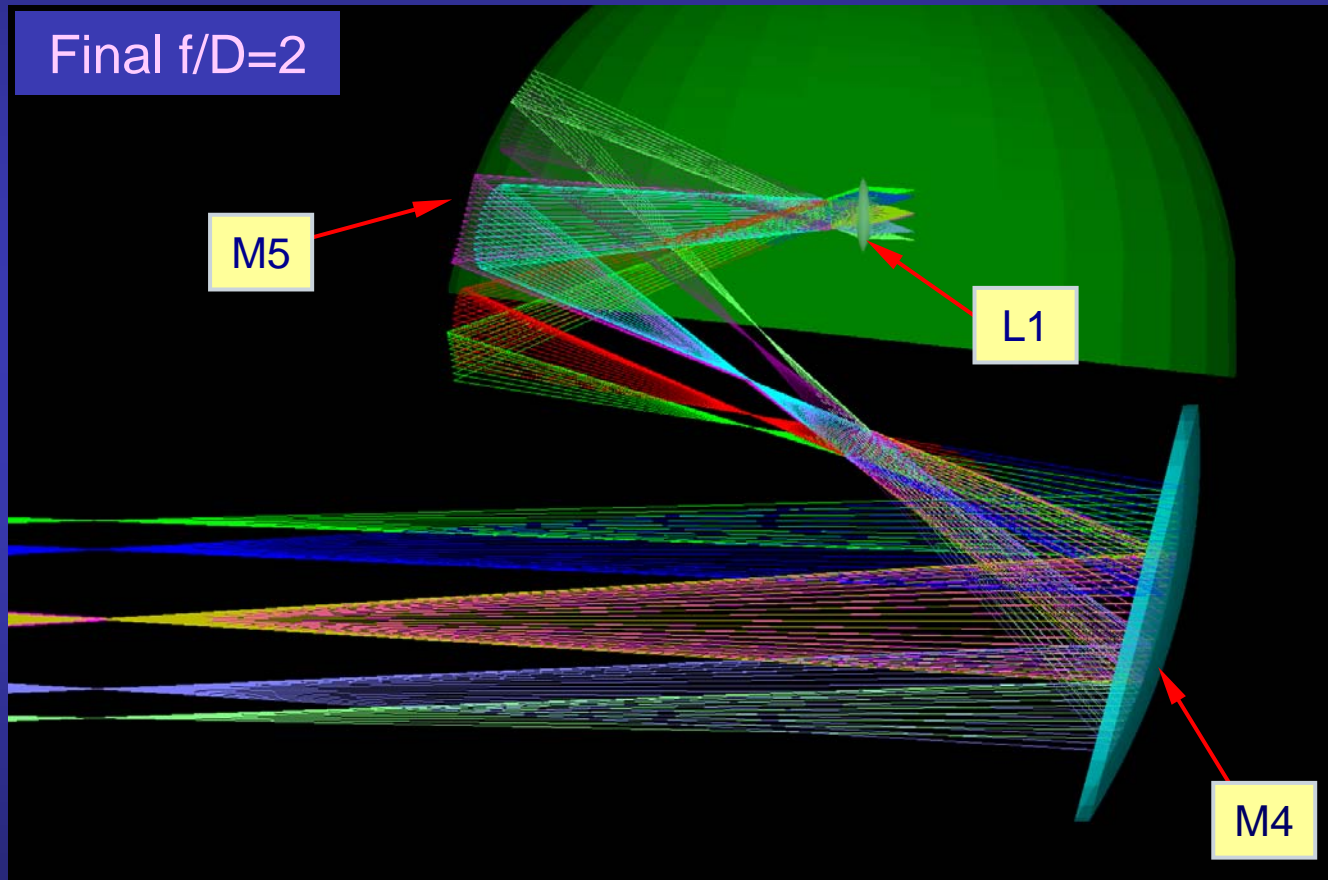
for 20' Diameter FOV,  $\theta_{inc}=15^\circ$ ,  $f_1/0.6$



LWCam  $f_1/0.6$ ,  $\theta_{inc}=15^\circ$ ,  $f/2$

# LW-Cam Re-imaging Optics

for 20' Diameter FOV,  $\theta_{inc}=15^\circ$ ,  $f_1/0.4$

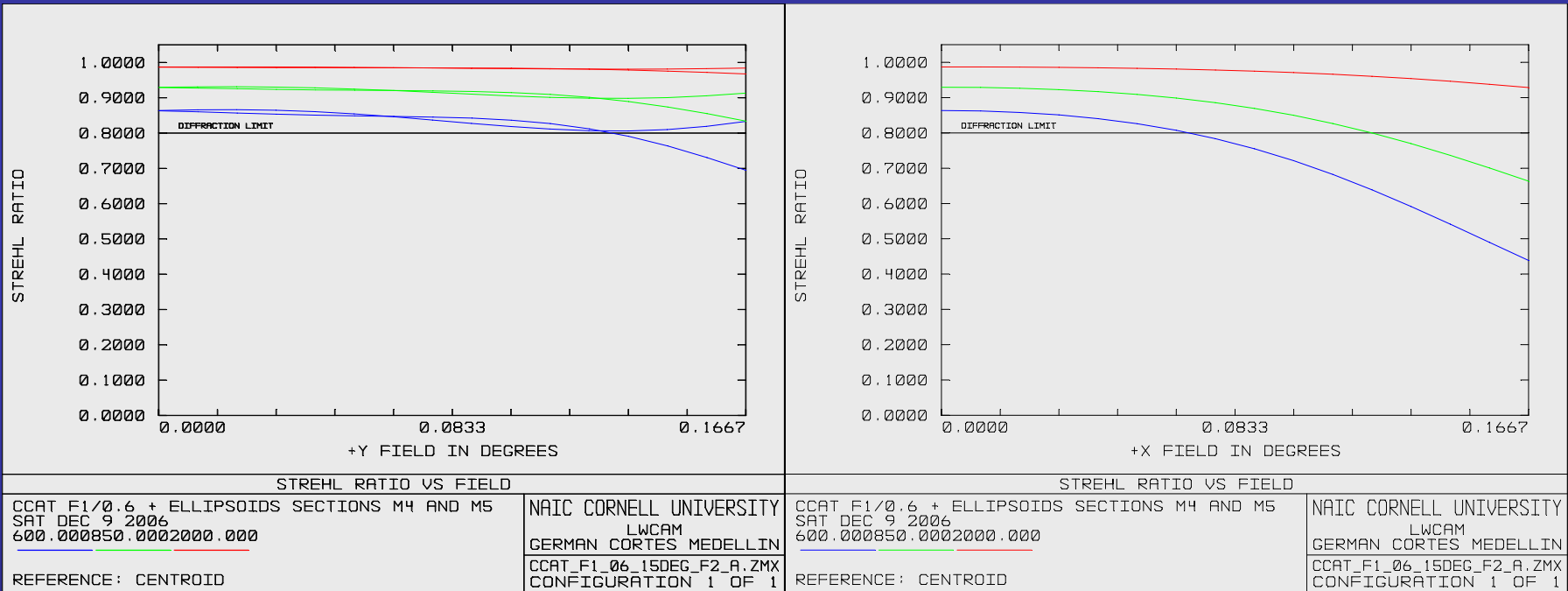


LWCam  $f_1/0.4$ ,  $\theta_{inc}=15^\circ$ ,  $f/2$

# LW-Cam **Strehl Ratio** over FOV

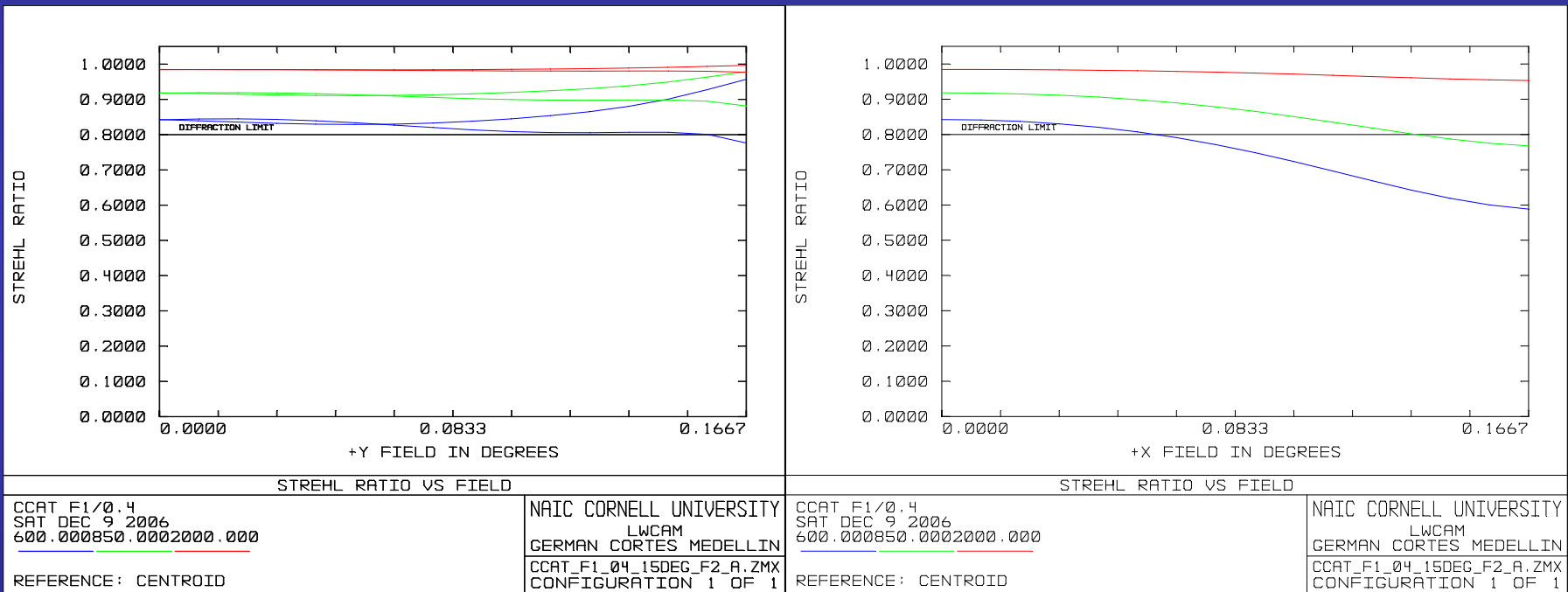


$$\theta_{\text{inc}} = 15^\circ, f_1/0.6$$



# LW-Cam **Strehl Ratio** over FOV

$$\theta_{\text{inc}} = 15^\circ, f_1/0.4$$

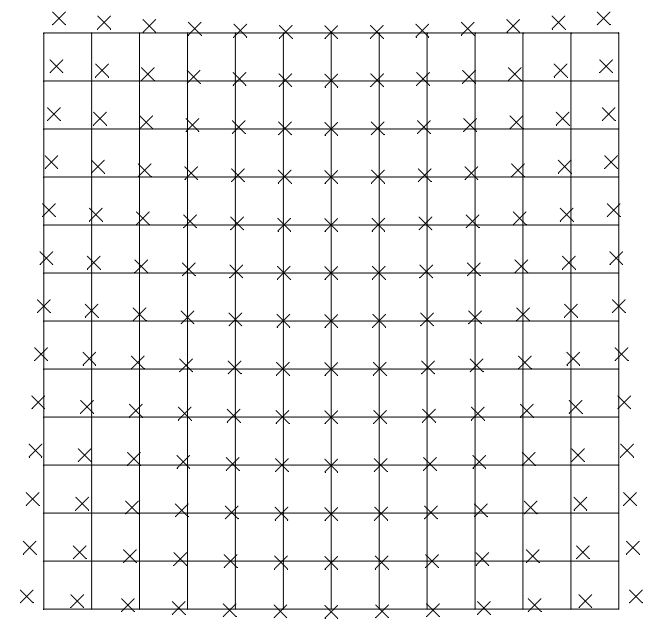




# LW-Cam **Distortion** over FOV

$$\theta_{inc} = 15^\circ, f_1/0.6$$

**f1/0.6: Max Distortion= 5.22 %**



GRID DISTORTION

CCAT F1/0.6 + ELLIPSOIDS SECTIONS M4 AND M5  
SAT DEC 9 2006  
FIELD: 0.2357 W 0.2357 H DEGREES  
IMAGE: 206.54 W 206.63 H MILLIMETERS  
MAXIMUM DISTORTION: 5.2222%  
SCALE: 1.000X, WAVELENGTH: 600.0000  $\mu\text{m}$

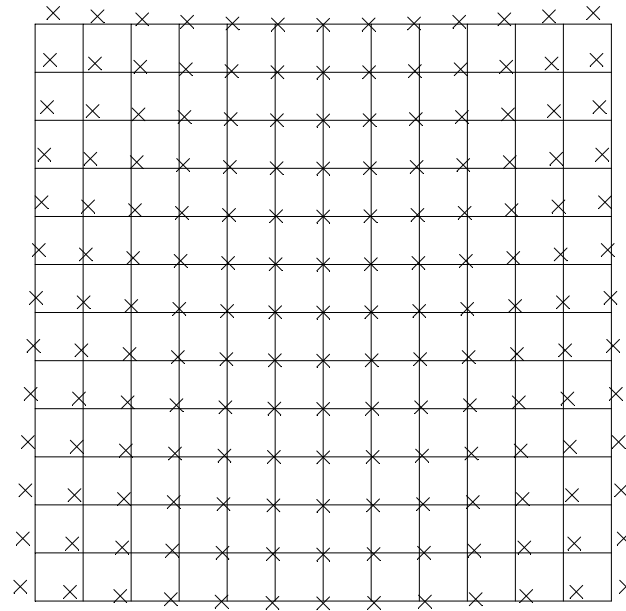
NAIC CORNELL UNIVERSITY  
LWCAM  
GERMAN CORTES MEDELLIN  
CCAT\_F1\_06\_15DEG\_F2\_A.ZMX  
CONFIGURATION 1 OF 1



# LW-Cam **Distortion** over FOV

$$\theta_{\text{inc}} = 15^\circ, f_1/0.4$$

**f1/0.4: Max Distortion= -5.21 %**



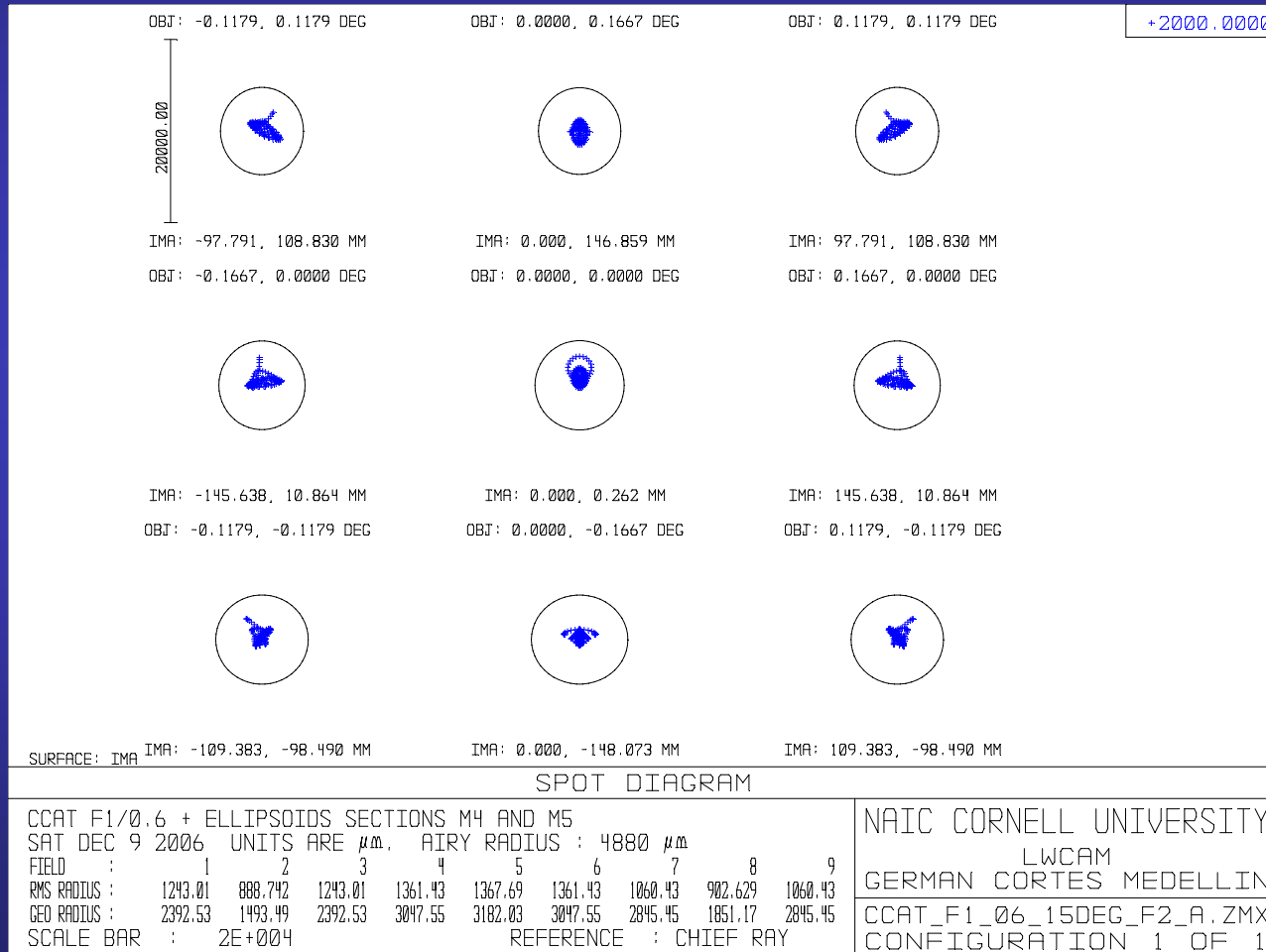
GRID DISTORTION

CCAT F1/0.4  
SAT DEC 9 2006  
FIELD: 0.2357 W 0.2357 H DEGREES  
IMAGE: 205.44 W 205.43 H MILLIMETERS  
MAXIMUM DISTORTION: -5.2141%  
SCALE: 1.000X, WAVELENGTH: 600.0000  $\mu\text{m}$

NAIC CORNELL UNIVERSITY  
LWCAM  
GERMAN CORTES MEDELLIN  
CCAT\_F1\_04\_15DEG\_F2\_A.ZMX  
CONFIGURATION 1 OF 1

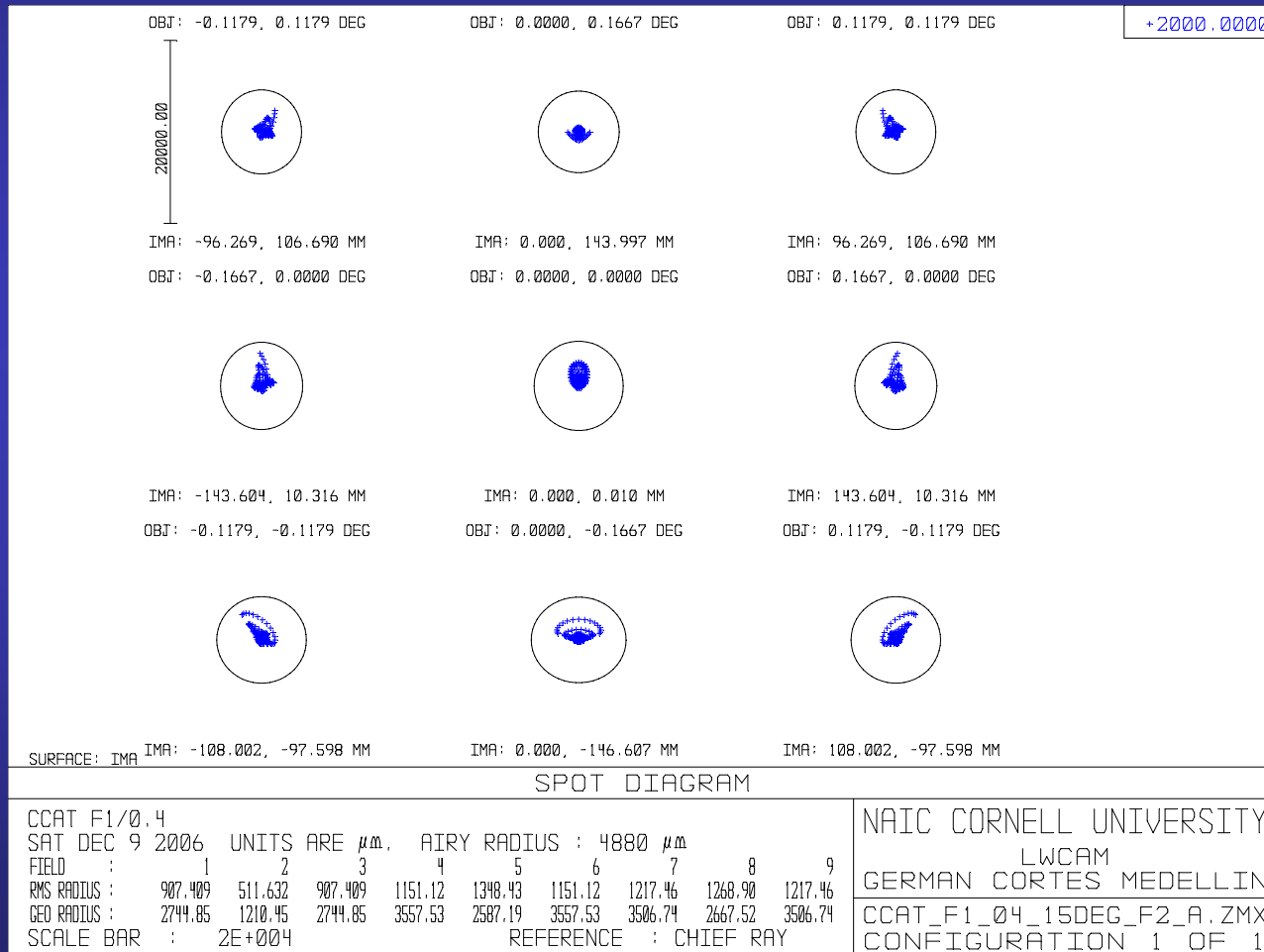
# LW-Cam Spot Diagram

$$\theta_{\text{inc}} = 15^\circ, f_1/0.6$$



# LW-Cam Spot Diagram

$$\theta_{\text{inc}} = 15^\circ, f_1/0.4$$







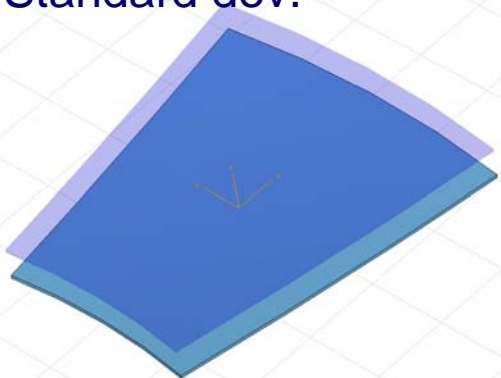
# Active Surface Segment Positioning Errors and Strehl

$f_1/0.6$  vs.  $f_1/0.4$

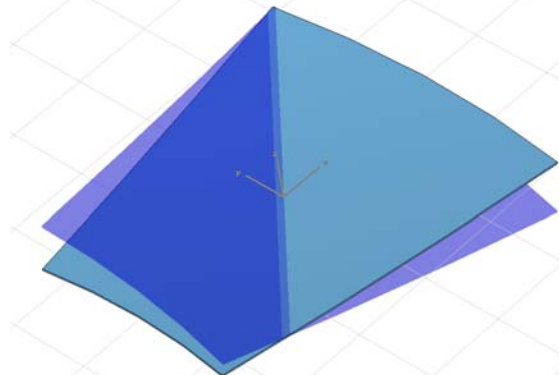
# Segment Positioning Errors $f_1/0.6$ vs. $f_1/0.4$



$\Delta z$ : Gaussian Distributed,  
zero mean  
 $\sigma_z$ : Standard dev.



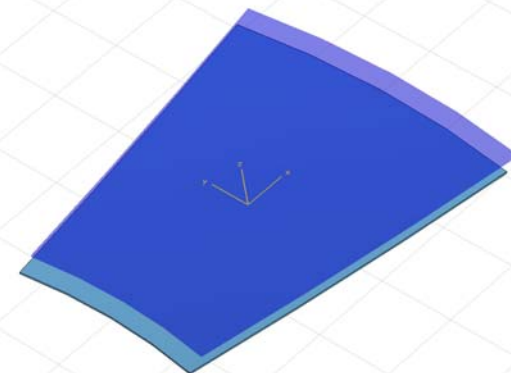
**PISTON**



**TILT/TIP**

$\Delta\phi$ : Uniform Distrib.  $[0, 2\pi]$   
 $\Delta\theta$ : Gaussian Distributed,  
zero mean  
 $\sigma_\theta$ : Standard dev.

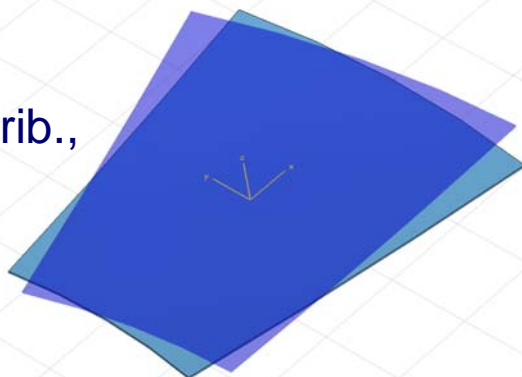
$\Delta x$ : Gaussian Distributed,  
zero mean  
 $\sigma_x$ : Standard dev.



**RADIAL**

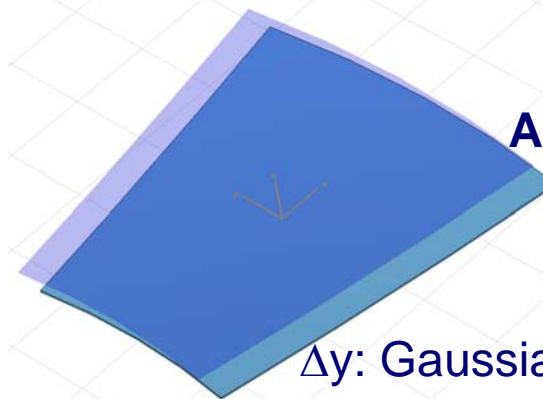
**TWIST**

$\Delta\omega$ : Gaussian Distrib.,  
zero mean  
 $\sigma_\omega$ : Standard dev.

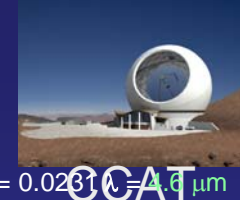


**AZIMUTH**

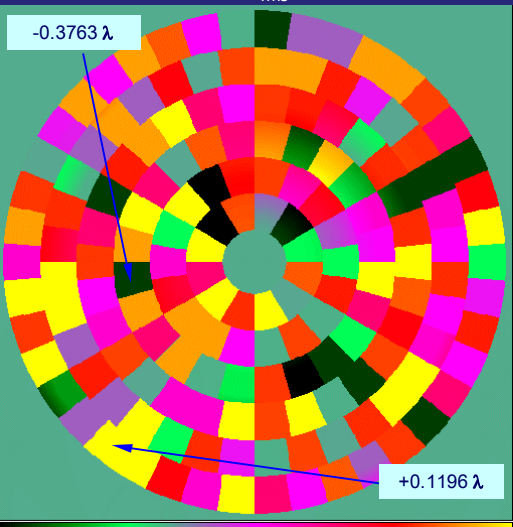
$\Delta y$ : Gaussian Distrib.  
zero mean  
 $\sigma_y$ : Standard dev.



# Segment Positioning Errors $f_1/0.6$ vs. $f_1/0.4$



Strehl= 89.6%  $\epsilon_{rms} = 0.0264\lambda = 5.7 \mu\text{m}$

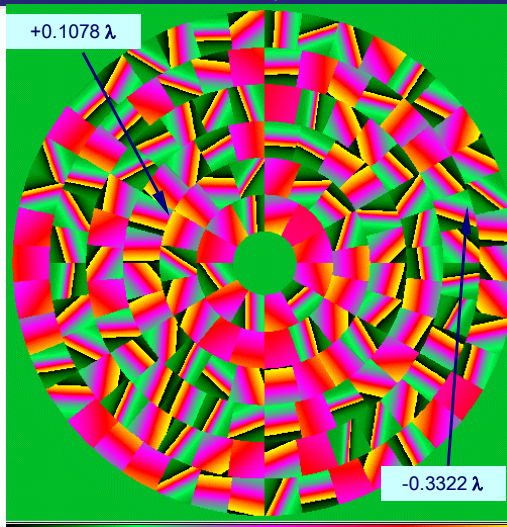


Aperture Phase Distribution [ $\lambda$ ]

**PISTON**

Strehl= 43.5%

Strehl= 80.7%  $\epsilon_{rms} = 0.0369\lambda = 7.4 \mu\text{m}$

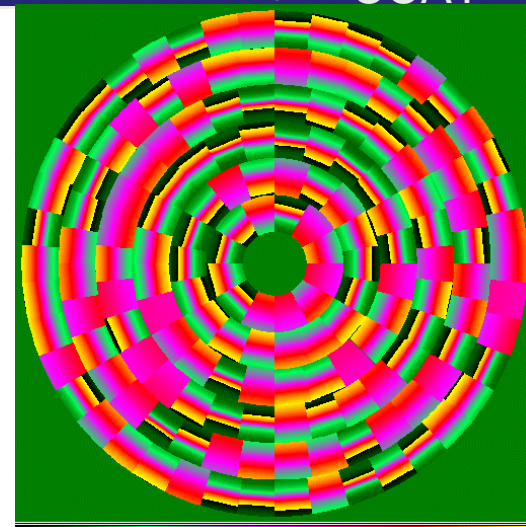


Aperture Phase Distribution [ $\lambda$ ]

**TILT/TIP**

14.5  $\mu\text{m}$  Strehl= 90.8%

Strehl= 91.9%  $\epsilon_{rms} = 0.0261\lambda = 5.4 \mu\text{m}$

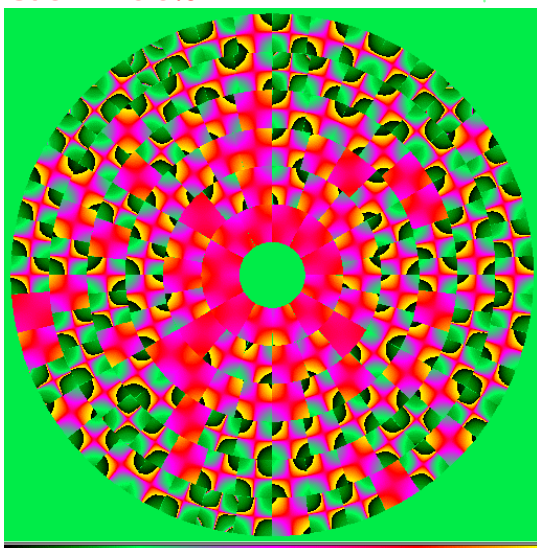


Aperture Phase Distribution [ $\lambda$ ]

**RADIAL**

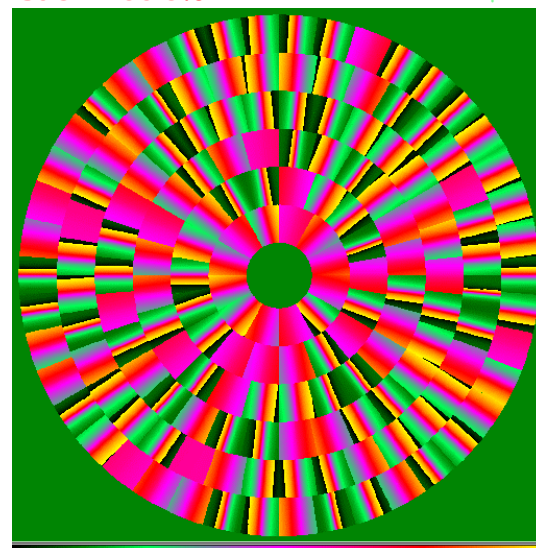
4.9  $\mu\text{m}$

**TWIST**



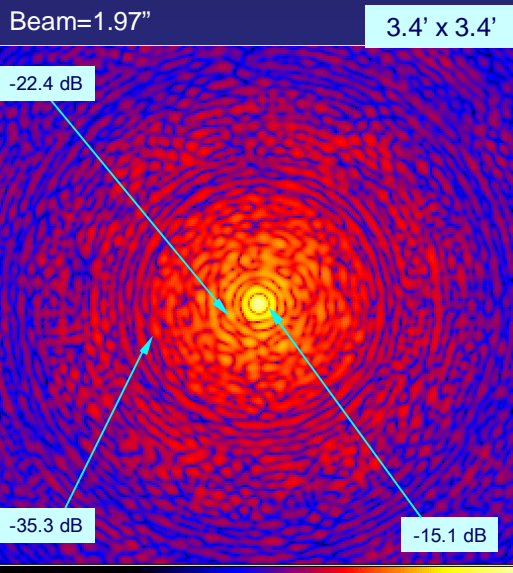
Aperture Phase Distribution [ $\lambda$ ]

**AZIMUTH**



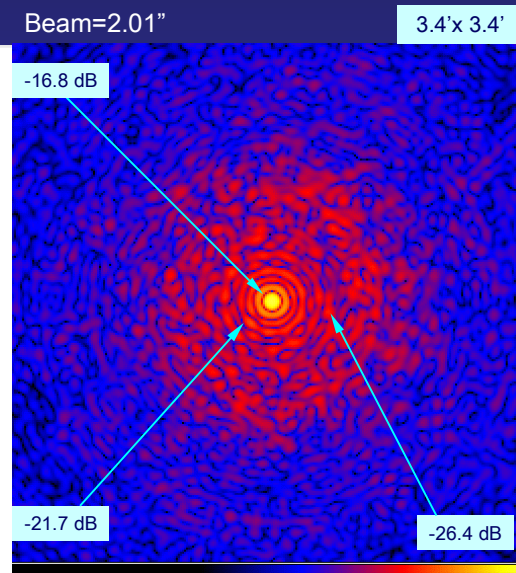
Aperture Phase Distribution [ $\lambda$ ]

# Segment Positioning Errors $f_1/0.6$ vs. $f_1/0.4$



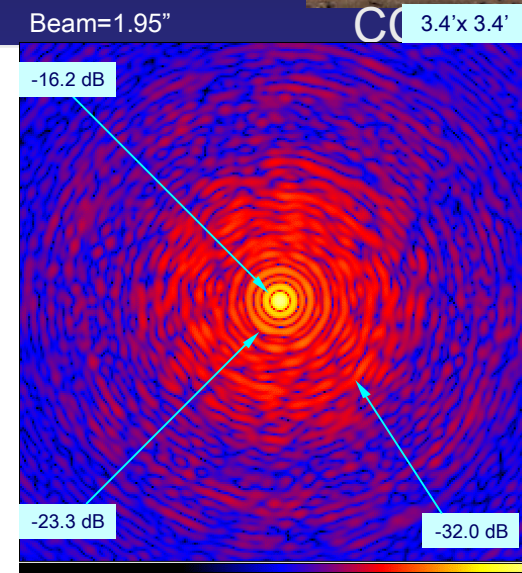
Far Field Radiation Pattern [dB]

**PISTON**



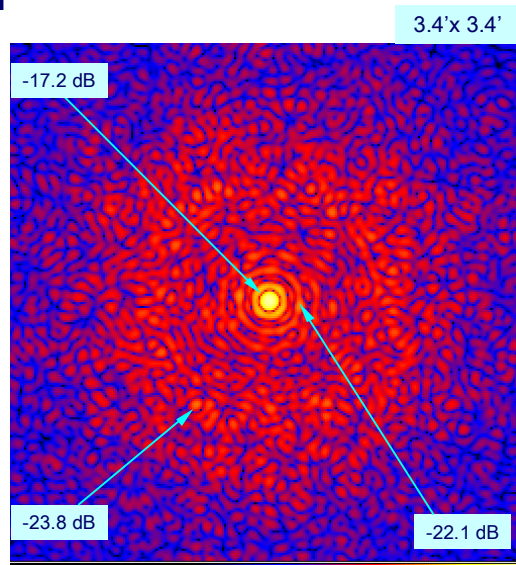
Far Field Radiation Pattern [dB]

**TILT/TIP**

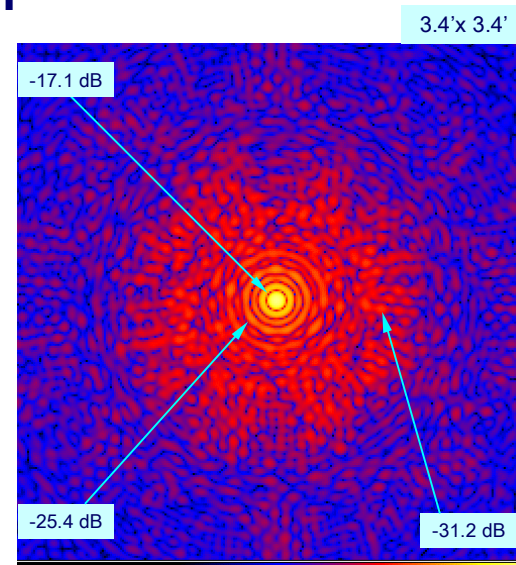


**RADIAL**

**TWIST**



Far Field Radiation Pattern [dB]

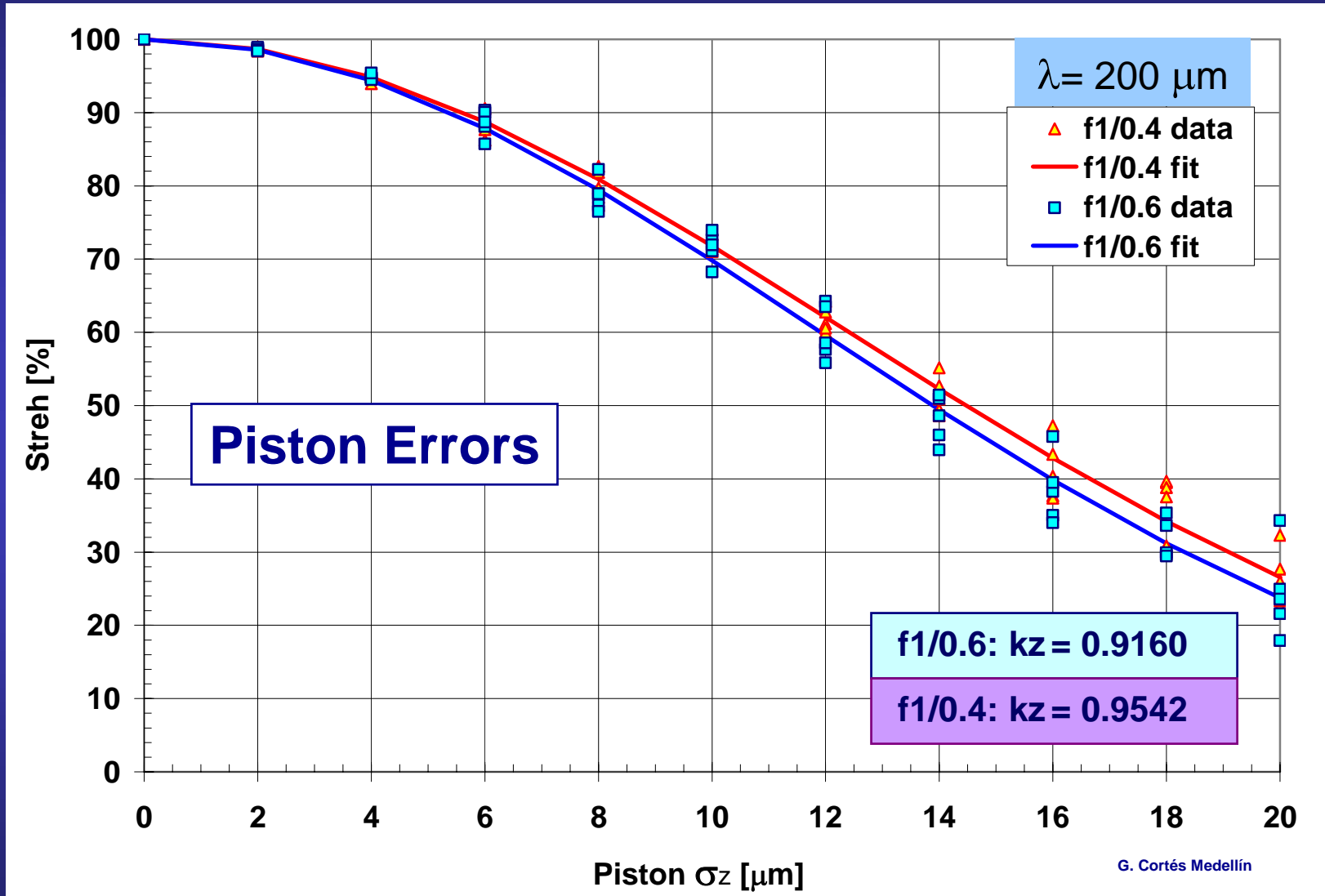


Far Field Radiation Pattern [dB]

**AZIMUTH**

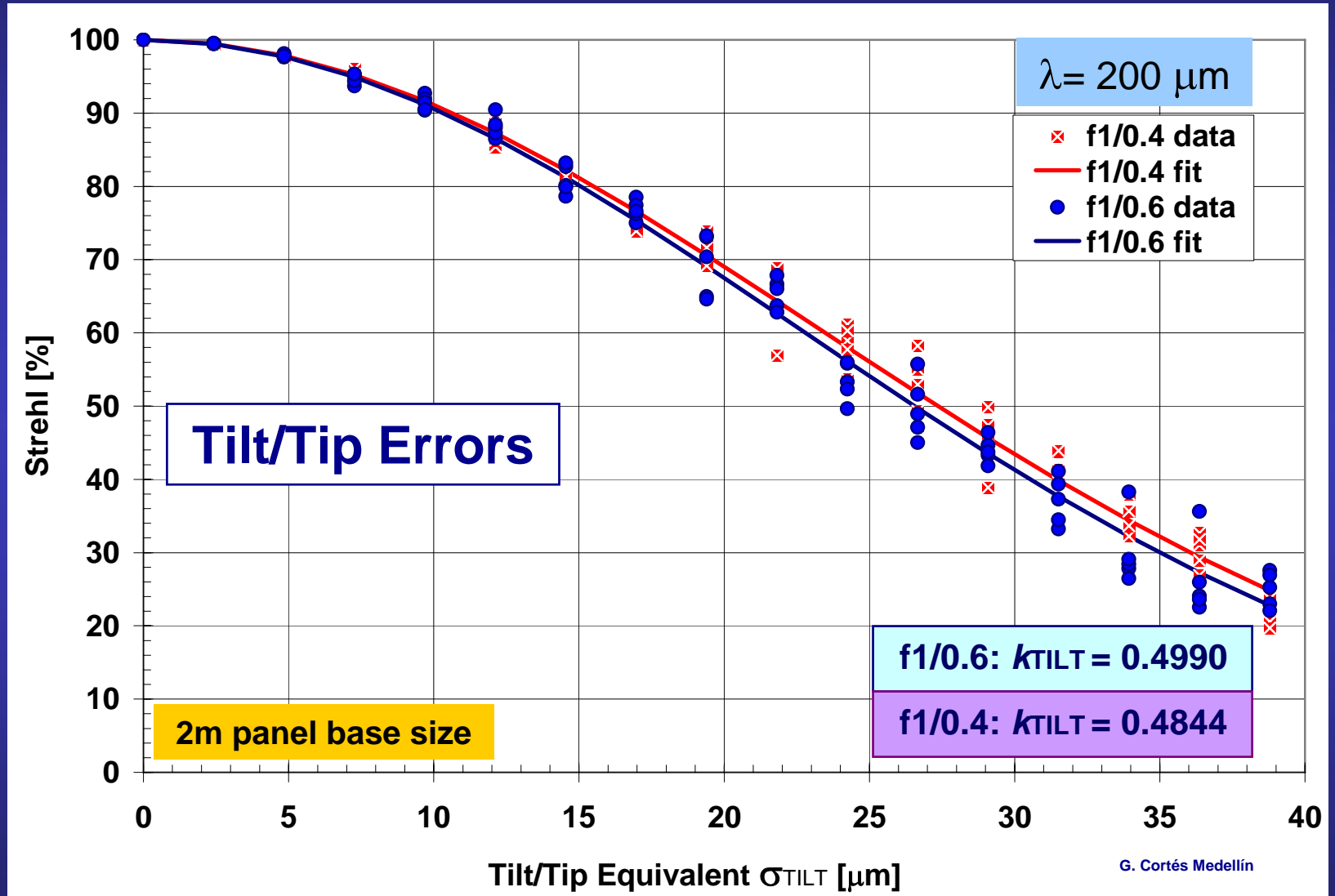
# Segment Piston Errors

$f_1/0.6$  vs.  $f_1/0.4$



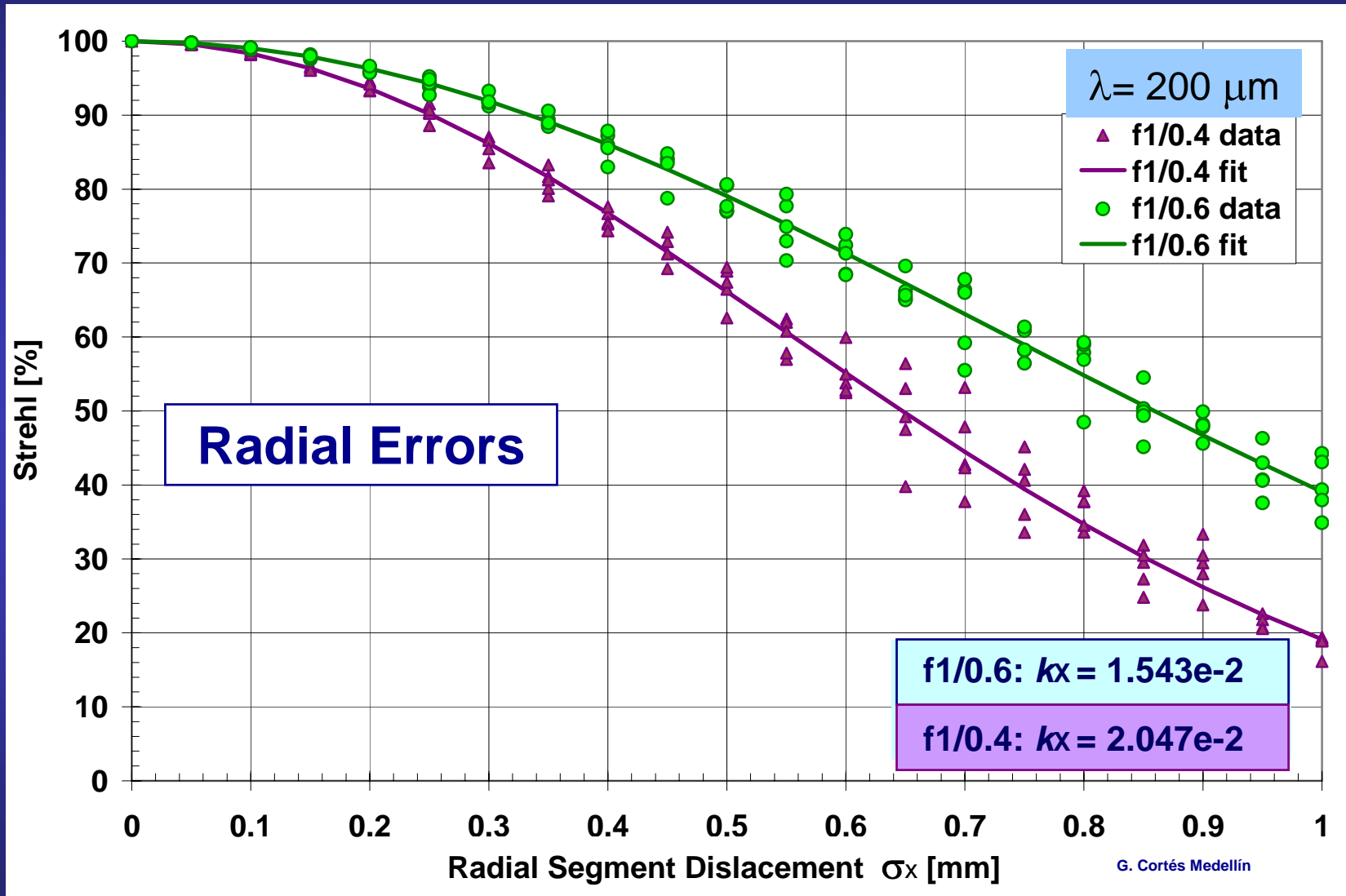
# Segment Tilt/Tip Errors

$f_1/0.6$  vs.  $f_1/0.4$



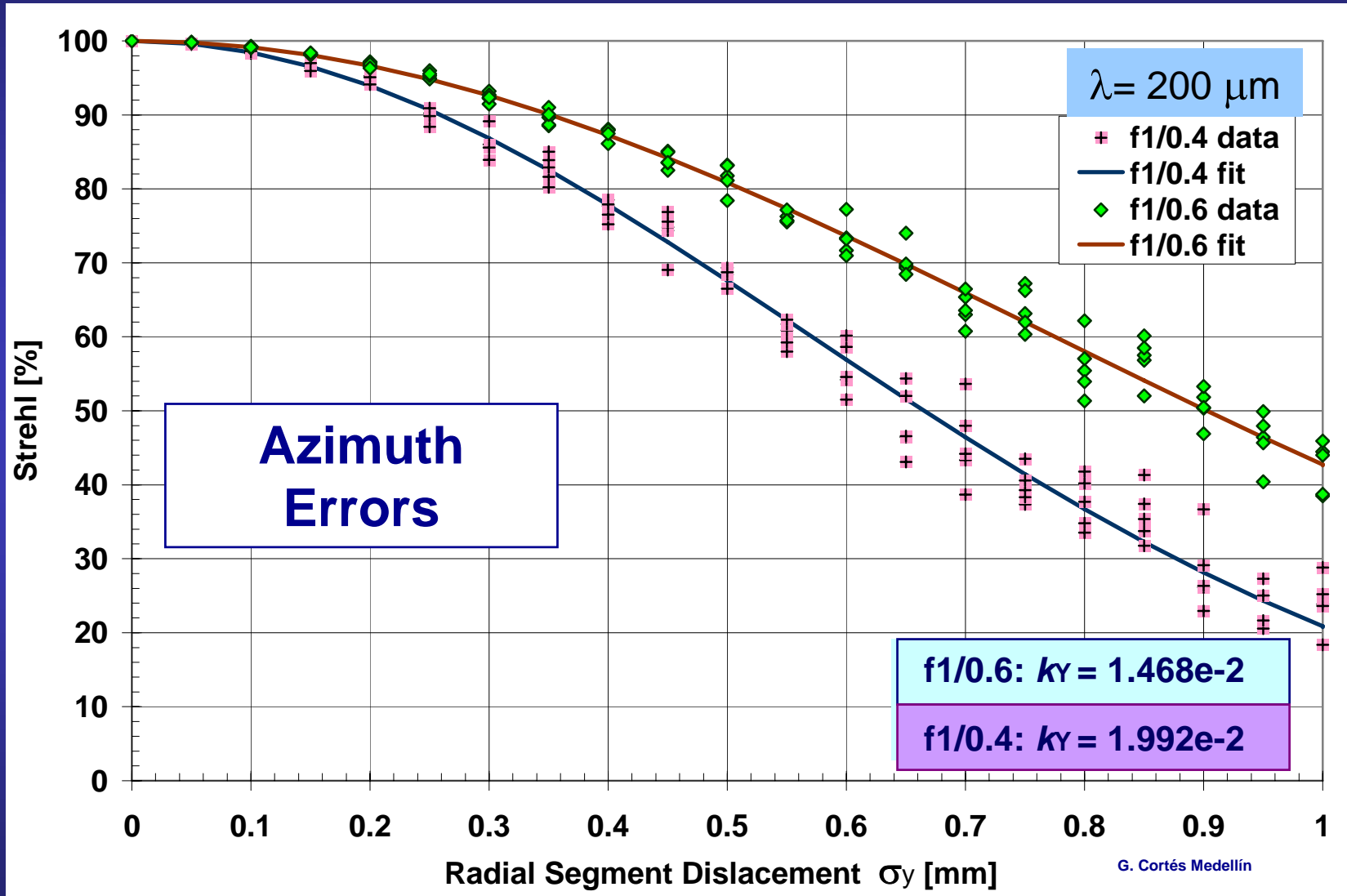
# Segment Radial Positioning Errors

$f_1/0.6$  vs.  $f_1/0.4$



# Segment Azimuth Positioning Errors

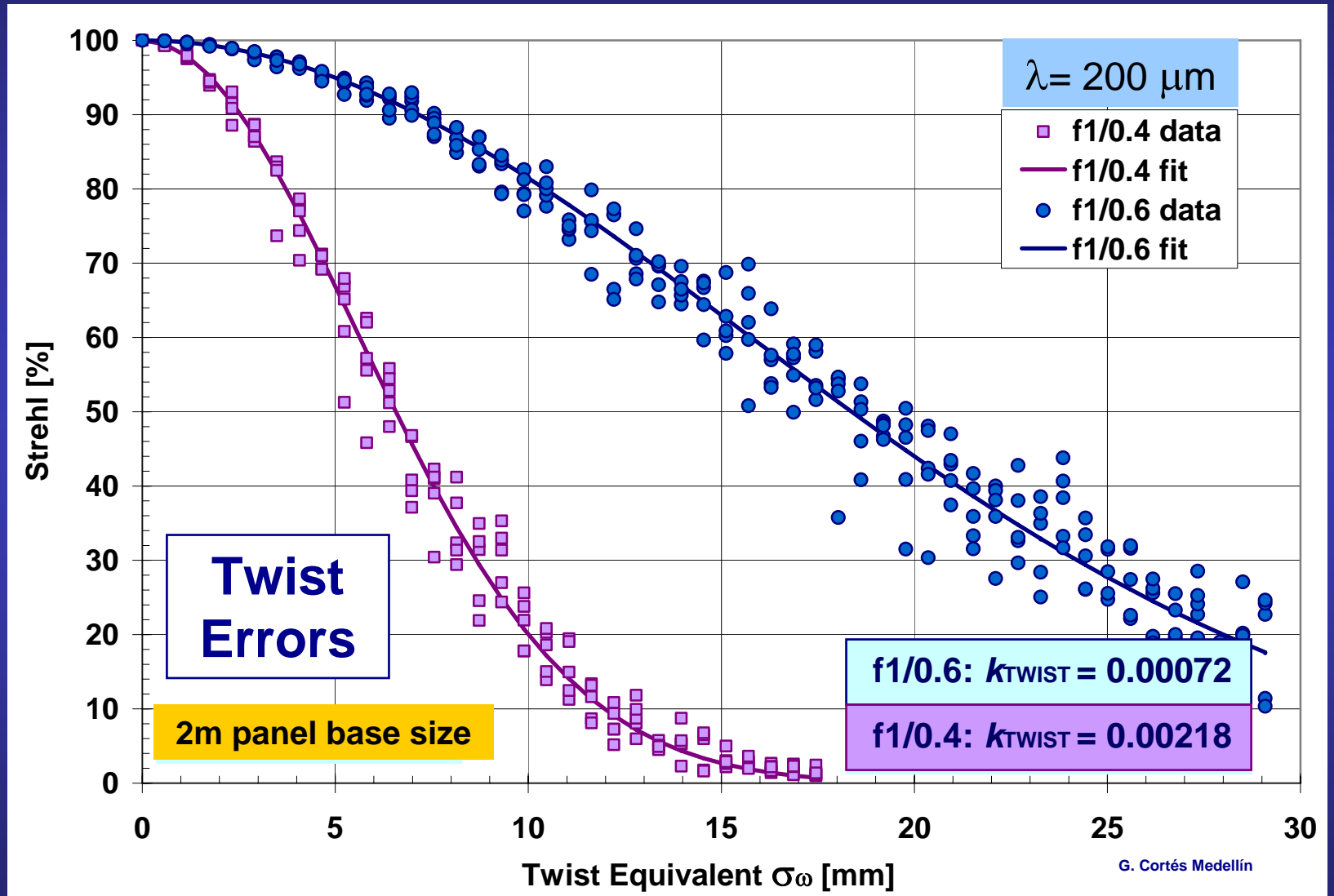
$f_1/0.6$  vs.  $f_1/0.4$





# Segment **Twist** Positioning Errors

$f_1/0.6$  vs.  $f_1/0.4$



# Best Fitted Ruze's Coefficients

$f_1/0.6$  vs.  $f_1/0.4$



## Ruze's Coefficient

$$\eta_{RUZE_i} = e^{-\left(\frac{4\pi \kappa_i \sigma_i}{\lambda}\right)^2}$$

Segment Piston Displacement  
 Segment Tilt/Tip (Equiv. Edge Displacement\*)  
 Segment Radial Displacement  
 Segment Azimuth Displacement  
 Segment Twist (Equiv. Edge Displacement\*)

Symbol	$f_1/0.6$	$f_1/0.4$
$\kappa_z$	0.95424	0.91602
$\kappa_{TILT}$	0.49903	0.48435
$\kappa_x$	0.01543	0.02047
$\kappa_y$	0.01468	0.01992
$\kappa_{TWIST}$	0.00073	0.00202

$$\epsilon_{rms} = \sqrt{(\kappa_z \sigma_z)^2 + (\kappa_{tilt} \sigma_{tilt})^2 + (\kappa_x \sigma_x)^2 + (\kappa_y \sigma_y)^2 + (\kappa_\omega \sigma_\omega)^2}$$

\* Panel Base Size = 2.0 [m]

# Conclusions II



## Segment Positioning Errors and Image Quality at $200\mu\text{m}$ :

- ◆ Again, piston errors dominate the contribution to Strehl, followed by tilt/tip segment errors.
- ◆ There is a slight reduction in Ruze's piston coefficient from 0.954 at  $f1/0.6$  to 0.916 at  $f1/0.4$
- ◆ There is also a slight reduction in Ruze's tilt/tip coefficient from 0.499 at  $f1/0.6$  to 0.484 at  $f1/0.4$ .
- ◆ In contrast, there is an increase in Ruze's coefficient for both, radial and azimuth segment positioning errors. For radial errors it changed from 0.0154 at  $f1/0.6$  to 0.0247 at  $f1/0.4$ , and for azimuth errors it changed from 0.0147 at  $f1/0.6$  to 0.0199 at  $f1/0.4$ , respectively.
- ◆ The largest change occurs in Ruze's twist coefficient by a factor of three: from 0.00073 at  $f1/0.6$  to 0.00202 at  $f1/0.4$ . In other words, in order to have 95% Strehl ratio at  $f1/0.6$ , twist **alignment errors should be 5mm** or less at the edges of a 2m base size panel; and with  $f1/0.4$ , they must be maintained **below 2mm**.



CCAT

End



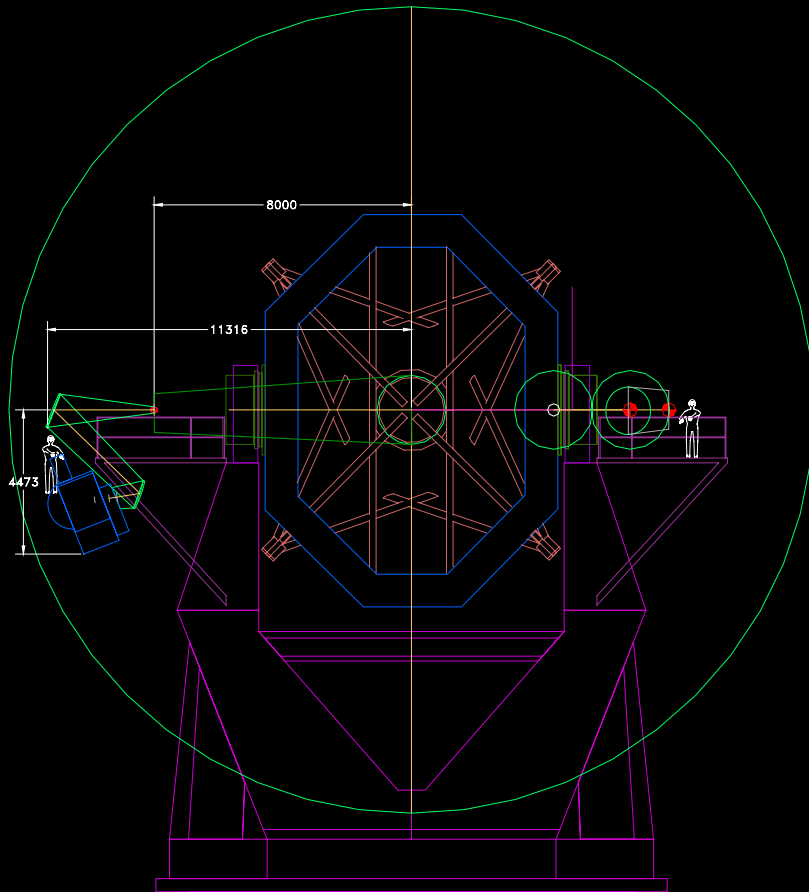
## Additional Material

# SCUBA-2 and SW/LW Camera Locations

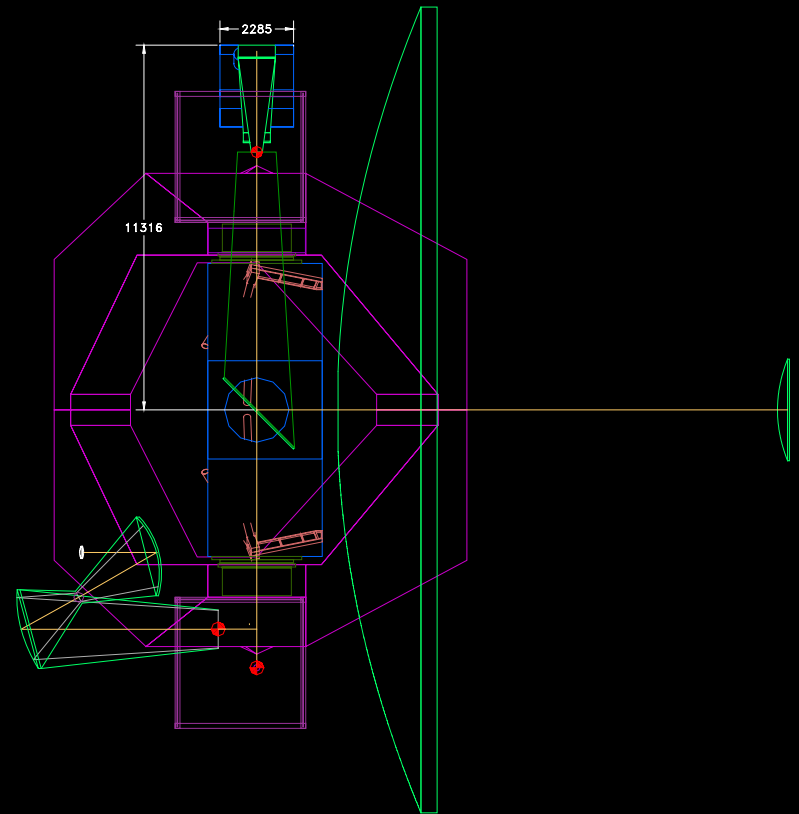


# SCUBA-2 Location I

Back View



Top View

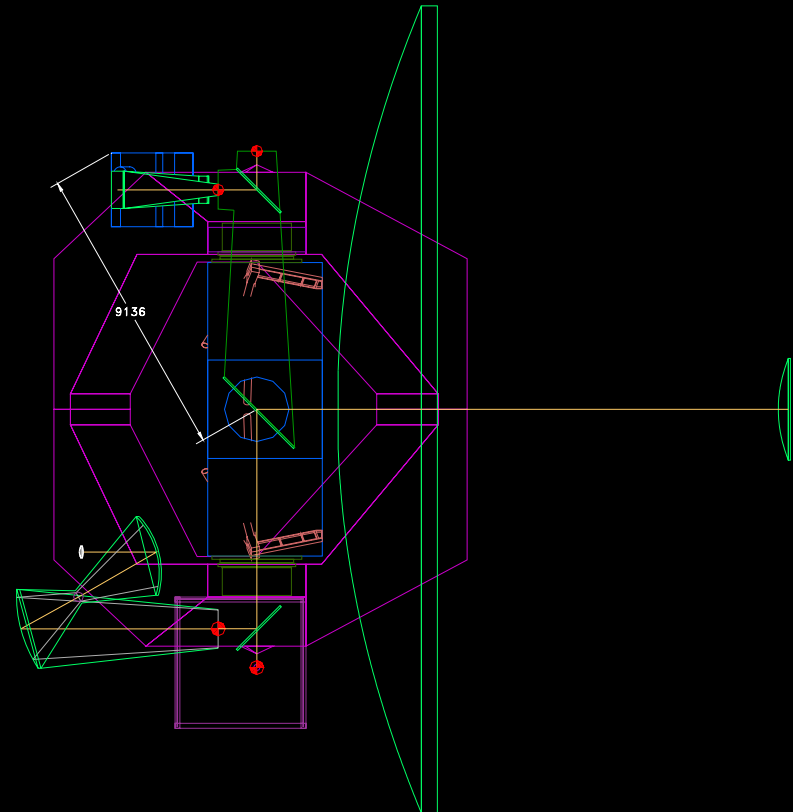
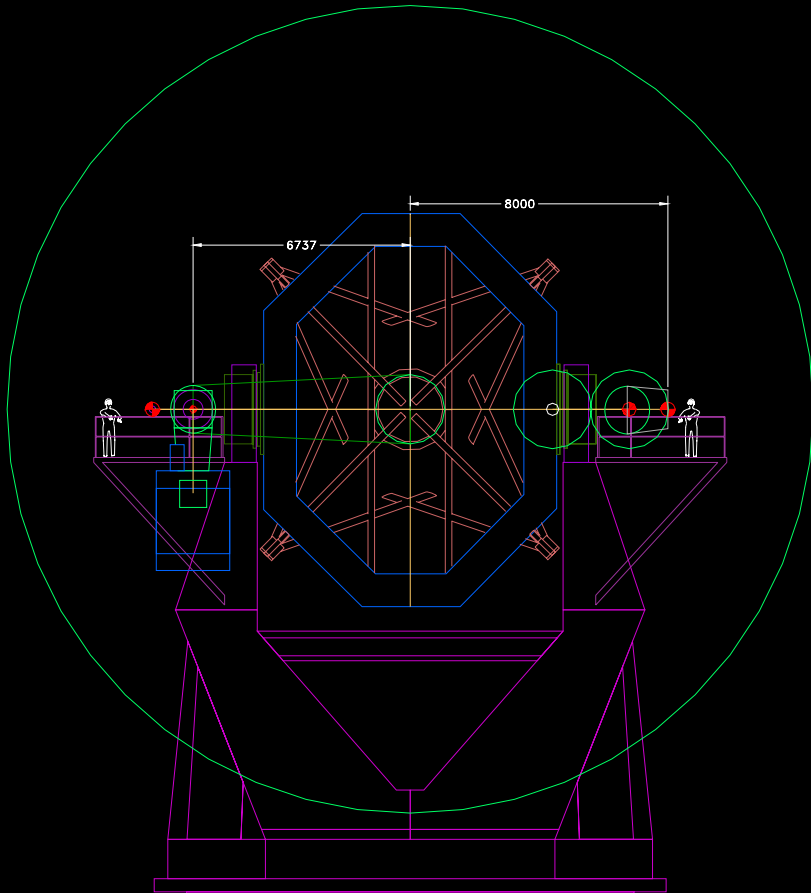




# SCUBA-2 Location II

Back View

Top View

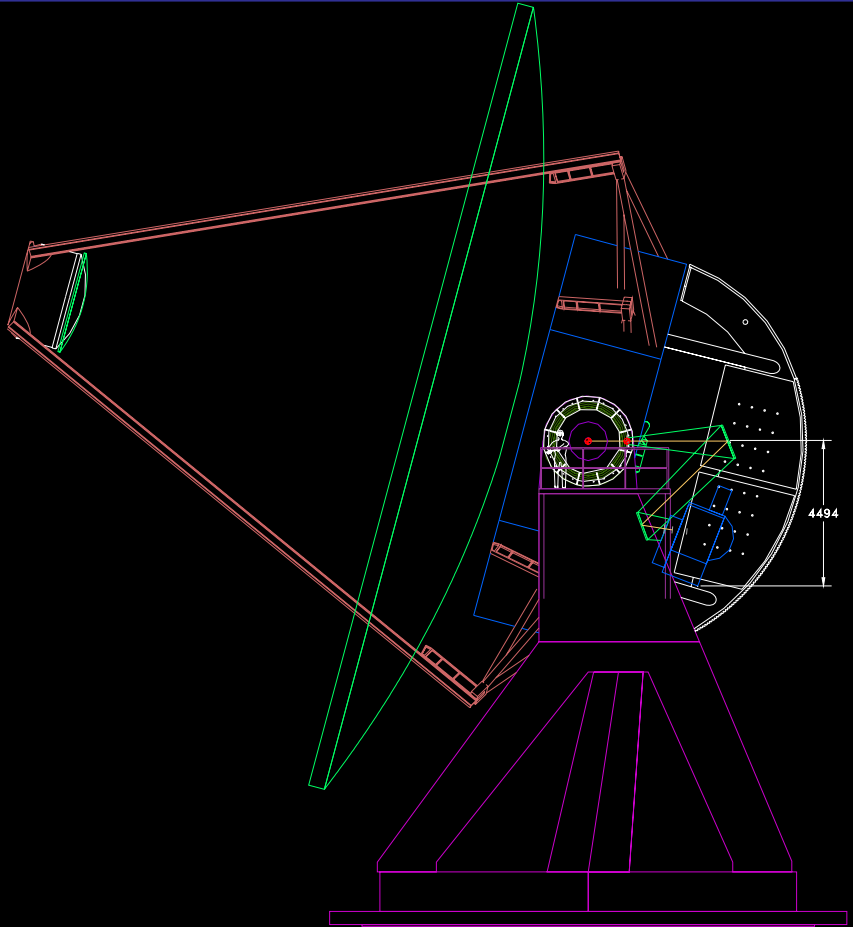
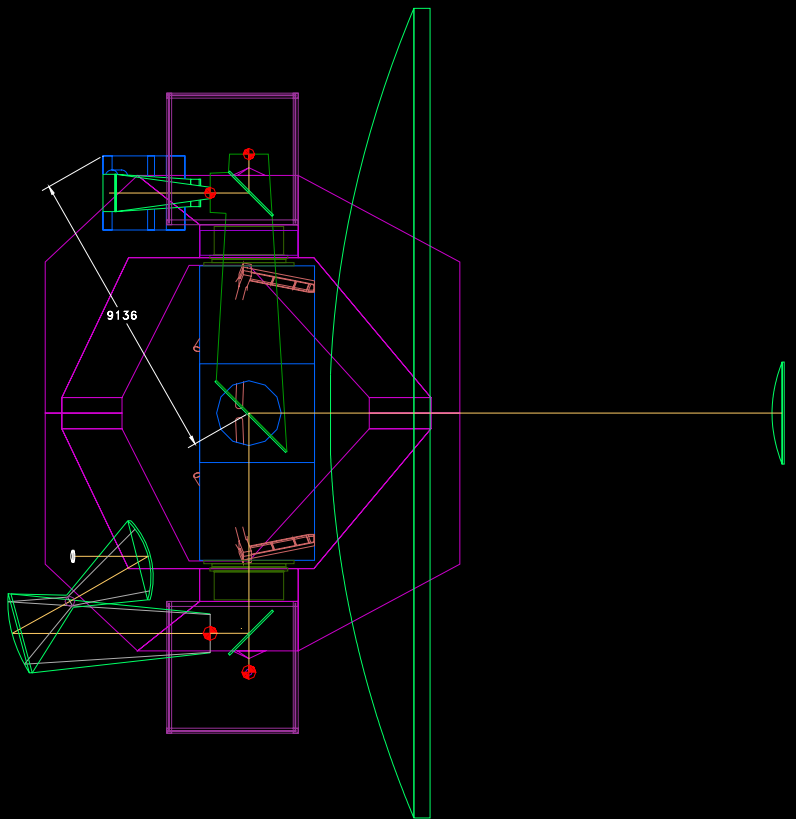




# SCUBA-2 Location II

Top View

Side View



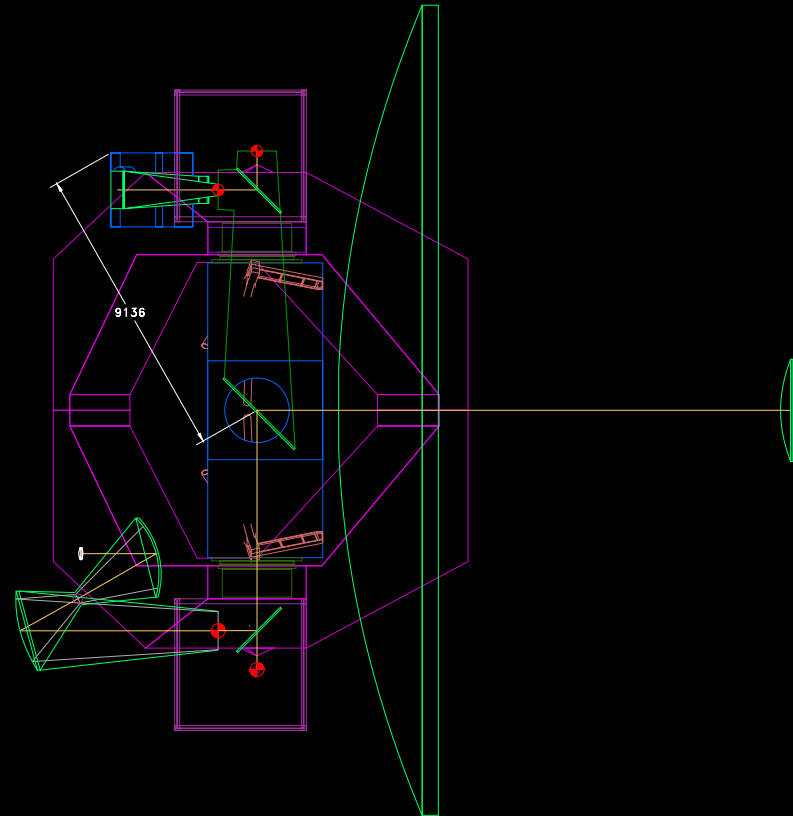
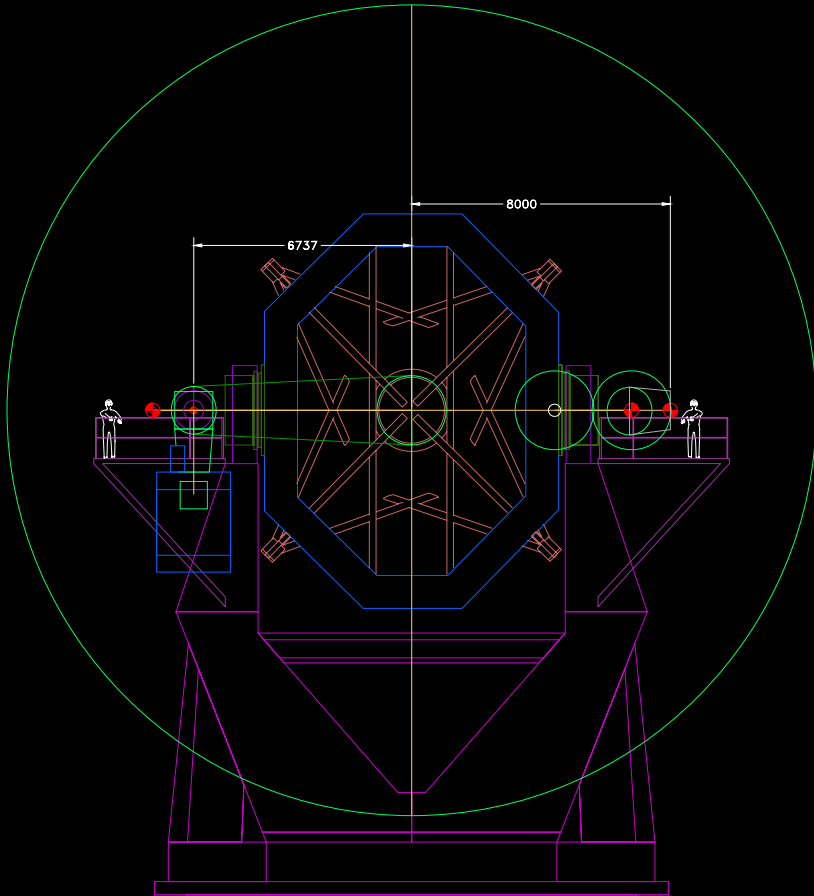




# SW-Cam + SCUBA-2 Location I

Back View

Top View

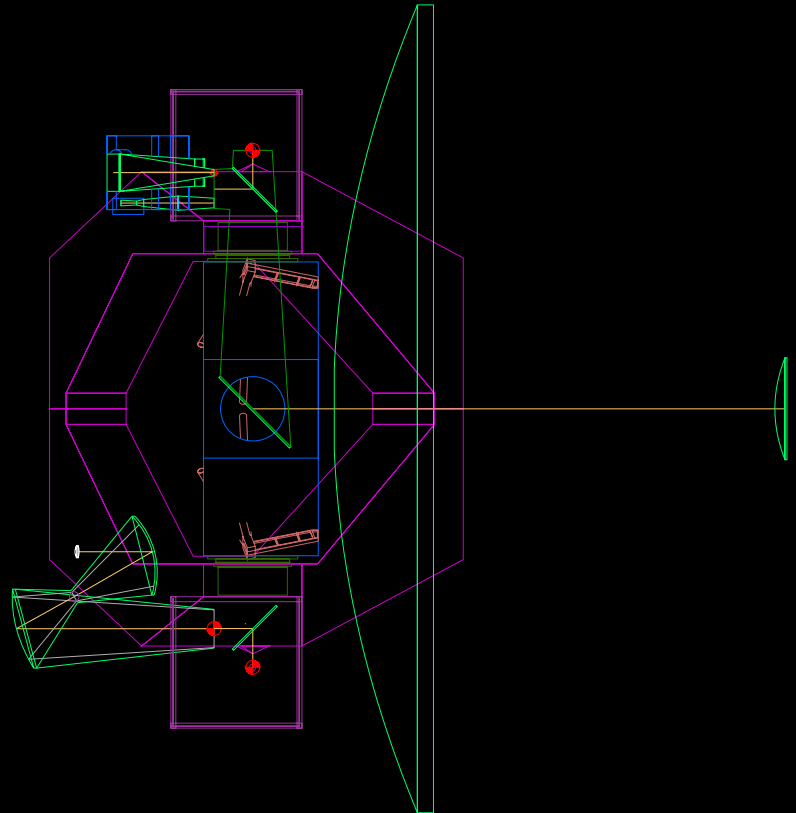
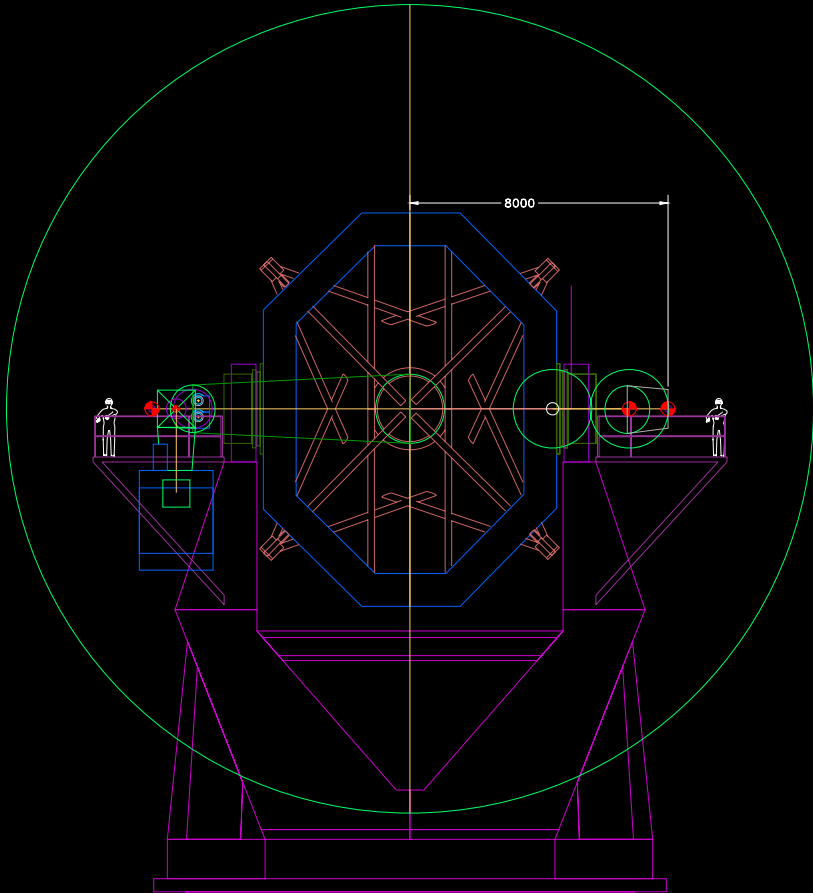




# SW-Cam + SCUBA-2 Location I

Back View

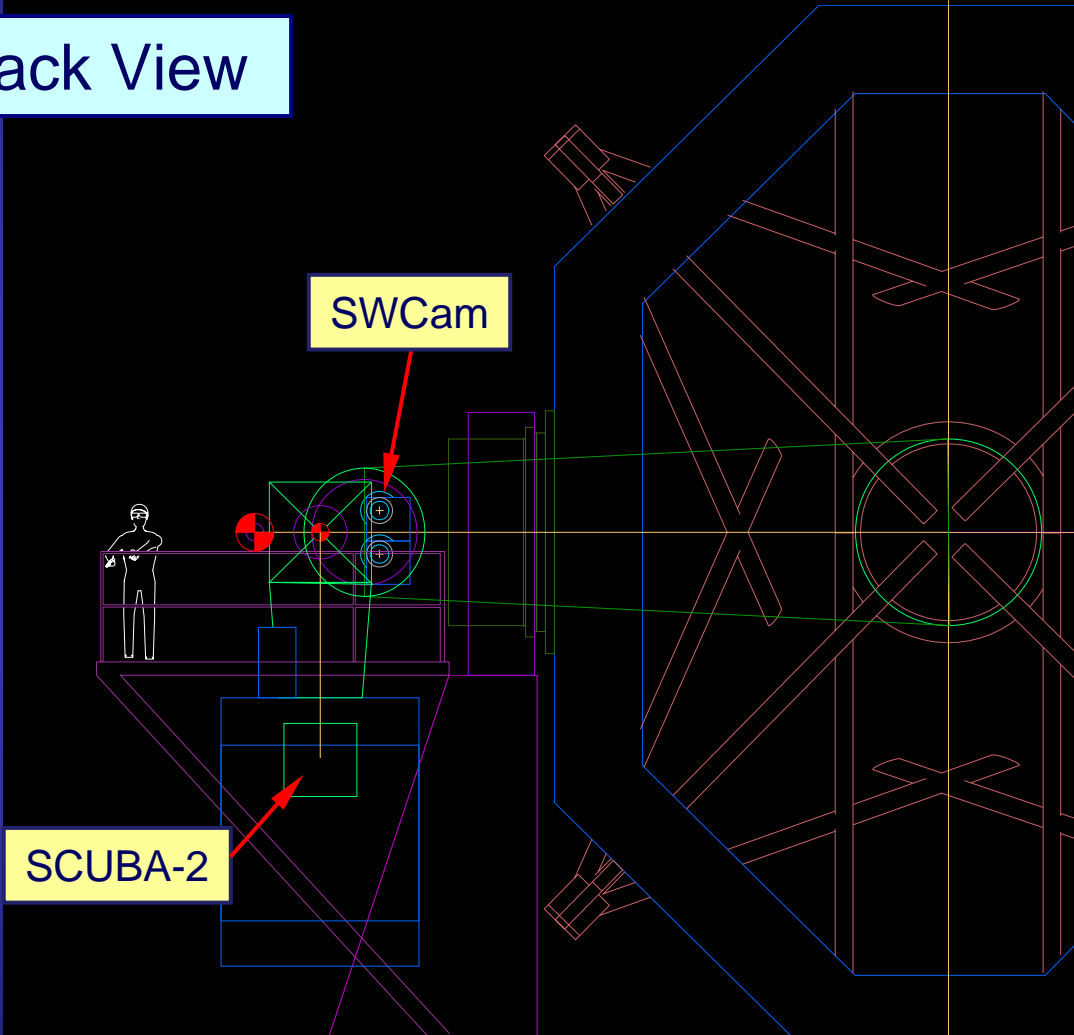
Top View





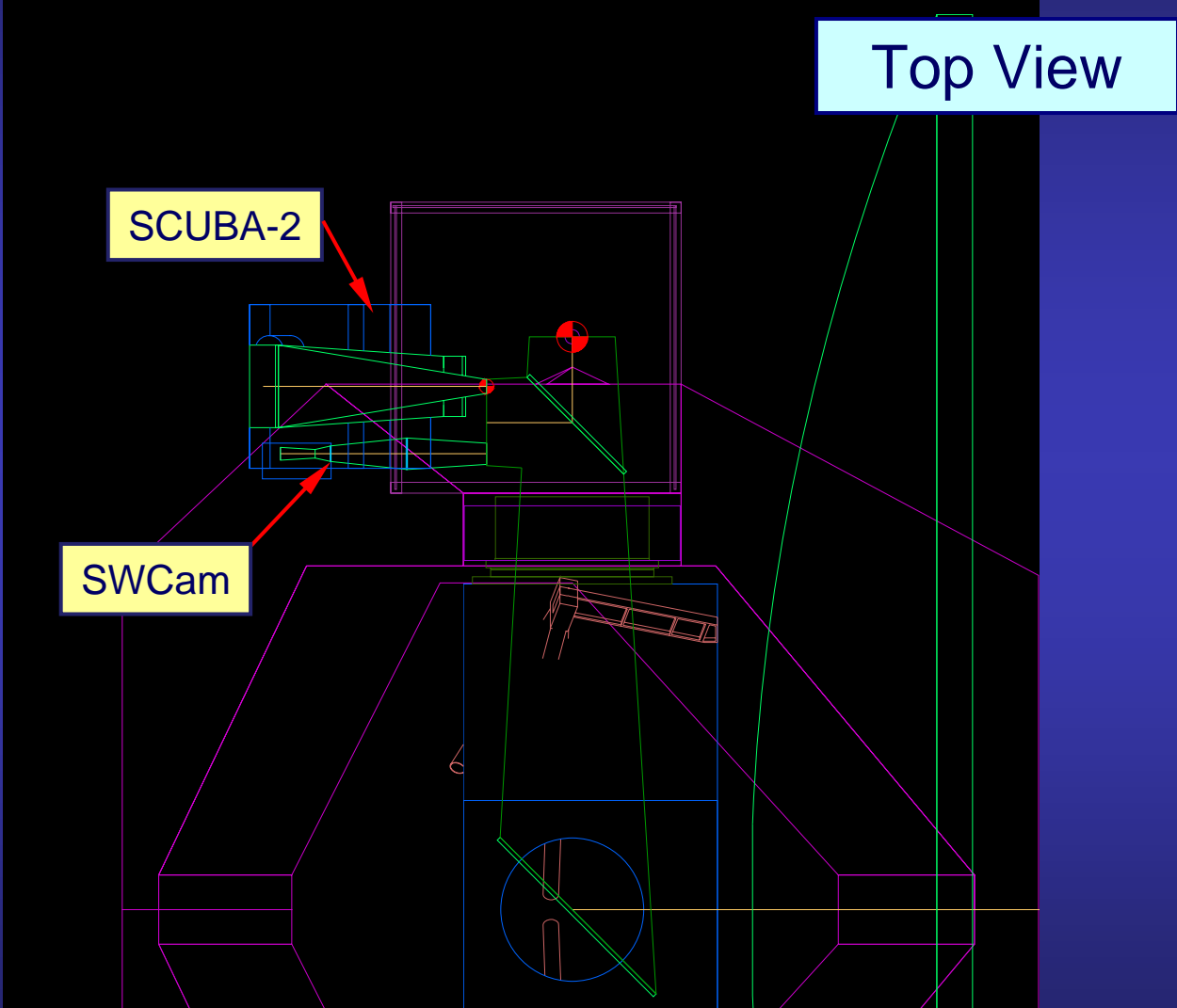
# SW-Cam + SCUBA-2 Location I

Back View



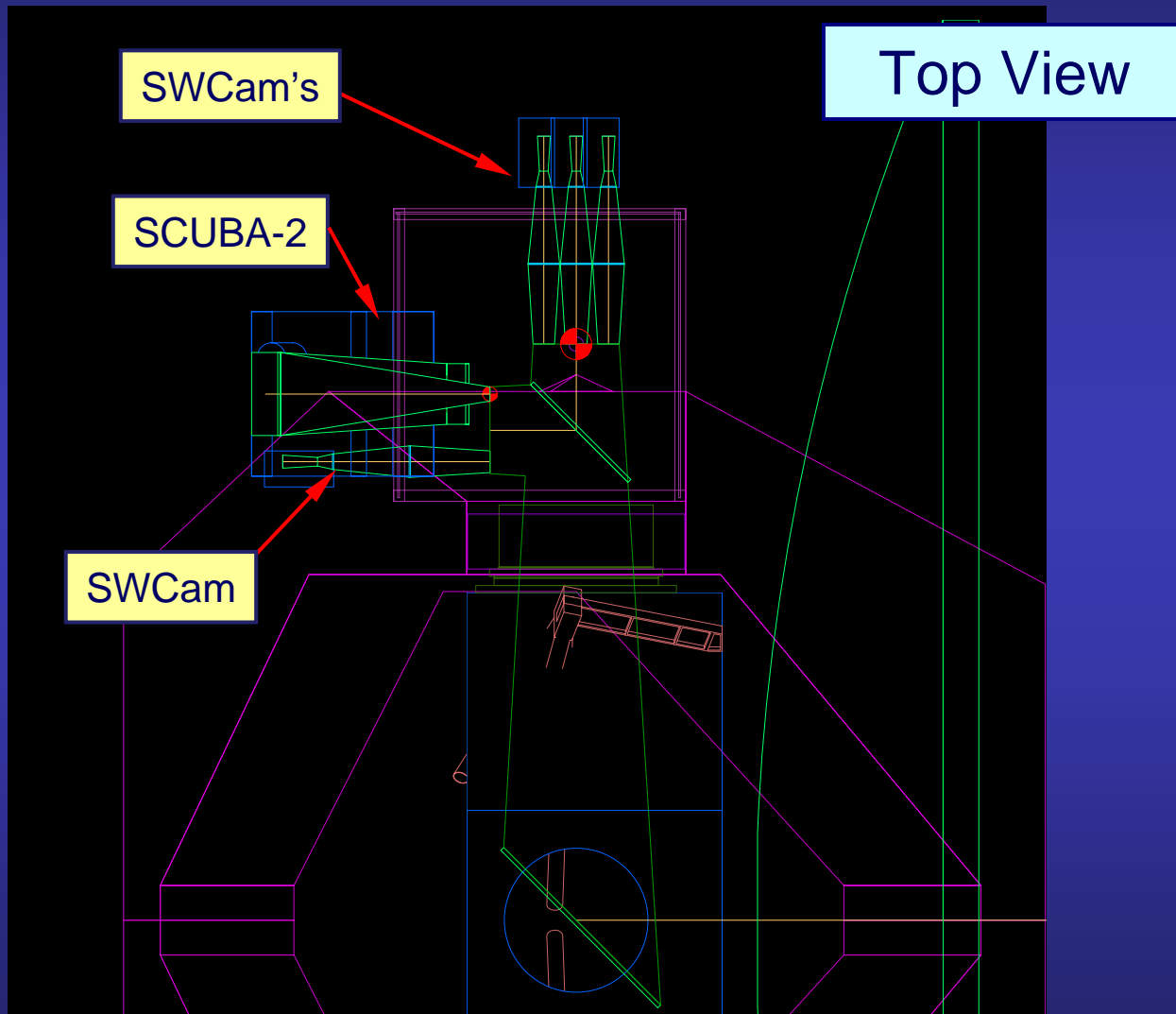


# SW-Cam + SCUBA-2 Location I





# SW-Cam + SCUBA-2 Location II





CCAT

End II